## v

## Romanian Master of Informatics 6th Edition, Bucharest, 10th - 13th of October 2018

## Colors

Consider a connected undirected graph with $N$ nodes and $M$ edges. Initially every node $u$ has a color $a[u]$, encoded by an integer between 1 and $N$. You can repeatedly modify node colors by assigning $a[u]=\min (a[u], a[v])$, where $u$ and $v$ are connected by an edge.

Given a destination coloring $b[1] \ldots b[N]$, determine whether you can transform $a$ into $b$.

## Input data

There are several test cases per input file and you should answer each of them separately.

The first line contains the number of test cases. Each test case is structured as

```
N M
a[1] a[2] ...a[N]
b[1] b[2] ... b[N]
```

$\mathrm{u}_{1} \mathrm{~V}_{1}$
$\mathrm{U}_{2} \mathrm{~V}_{2}$
$\mathrm{U}_{\mathrm{M}} \mathrm{V}_{\mathrm{M}}$

## Output data

For every test case you should print, on a separate line, 1 if $a$ can be transformed into $b$ using the above-mentioned operation and 0 otherwise.

## Limits and constraints

- For all test cases, $N \leq 150,000$ and $M \leq 200,000$.
- For every input file, the sum of all $N \leq 300,000$ and the sum of all $M \leq 400,000$.
- $1 \leq a[i], \mathrm{b}[i] \leq N$ for all $1 \leq i \leq N$.
- Time limit: 3.0 seconds
- Memory limit: 512 MB

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## Subtasks

Each subtask will be scored as a group. In order, the subtasks are:

| Subtask | Points | Additional input constraints |
| :--- | :--- | :--- |
| 1 | $15 \%$ | The graph is a star $(M=N-1$ and one node is connected to every other node). <br> The sum of $N^{2}$ among all test cases in an input file $\leq 5,000,000$. |
| 2 | $7 \%$ | The graph is complete. <br> $N \leq 50$. <br> The sum of $N \times M$ among all test cases in an input file $\leq 12,000,000$. |
| 3 | $8 \%$ | The graph is a chain $(M=N-1$ and the edges form a single path). <br> The sum of $N^{2}$ among all test cases in an input file $\leq 5,000,000$. |
| 4 | $15 \%$ | The graph is a chain, no further constraints. |
| 5 | $7 \%$ | The graph is a tree. <br> The sum of $N^{2}$ among all test cases in an input file $\leq 5,000,000$. |
| 6 | $16 \%$ | The graph is a tree and the coloring $a$ is a permutation of $\{1,2, \ldots, N\}$. |
| 7 | $10 \%$ | The sum of $N \times M$ among all test cases in an input file $\leq 5,000,000$. |
| 8 | $22 \%$ | none |

## Example

| Input | Output | Explanation |
| :--- | :--- | :--- |
| 2 | 1 | For the first graph, the operations needed are: |
| 44 | 0 | $a[2]=\min (a[2], a[3])=2$ |
| 3 | 2 | 1 |
| 2 | 2 | 1 |
| 12 |  | $a[1]=\min (a[1], a[2])=2$ |
| 23 |  | $a[2]=\min (a[2], a[4])=1$ |
| 3 | 4 |  |
| 42 |  |  |
| 44 |  |  |
| 3 | 321 |  |
| 122 | 1 |  |
| 12 |  |  |
| 23 |  |  |
| 3 | 4 |  |
| 42 |  |  |

