#### **International Olympiad in Informatics 2015**



26th July - 2nd August 2015 Almaty, Kazakhstan Day 1

teams

Language: en-ISC

# **Teams**

There is a class of N students, numbered 0 through N-1. Every day the teacher of the class has some projects for the students. Each project has to be completed by a team of students within the same day. The projects may have various difficulty. For each project, the teacher knows the exact size of a team that should work on it.

Different students may prefer different team sizes. More precisely, student i can only be assigned to a team of size between A[i] and B[i] inclusive. On each day, a student may be assigned to at most one team. Some students might not be assigned to any teams. Each team will work on a single project.

The teacher has already chosen the projects for each of the next Q days. For each of these days, determine whether it is possible to assign students to teams so that there is one team working on each project.

## **Example**

Suppose there are N=4 students and Q=2 days. The students' constraints on team sizes are given in the table below.

student	0	1	2	3
$\boldsymbol{A}$	1	2	2	2
В	2	3	3	4

On the first day there are M = 2 projects. The required team sizes are K[0] = 1 and K[1] = 3. These two teams can be formed by assigning student 0 to a team of size 1 and the remaining three students to a team of size 3.

On the second day there are M=2 projects again, but this time the required team sizes are K[0]=1 and K[1]=1. In this case it is not possible to form the teams, as there is only one student who can be in a team of size 1.

### Task

You are given the description of all students: N, A, and B, as well as a sequence of Q questions — one about each day. Each question consists of the number M of projects on that day and a sequence K of length M containing the required team sizes. For each question, your program must return whether it is possible to form all the teams.

You need to implement the functions init and can:

- init (N, A, B) The grader will call this function first and exactly once.
  - N: the number of students.

- A: an array of length N: A[i] is the minimum team size for student i.
- B: an array of length N: B[i] is the maximum team size for student i.
- The function has no return value.
- You may assume that  $1 \le A[i] \le B[i] \le N$  for each i = 0, ..., N-1.
- lacktriangledown can (M, K) After calling init once, the grader will call this function Q times in a row, once for each day.
  - M: the number of projects for this day.
  - K: an array of length M containing the required team size for each of these projects.
  - The function should return 1 if it is possible to form all the required teams and 0 otherwise.
  - You may assume that  $1 \le M \le N$ , and that for each i = 0, ..., M-1 we have  $1 \le K[i] \le N$ . Note that the sum of all K[i] may exceed N.

#### **Subtasks**

Let us denote by  $oldsymbol{S}$  the sum of values of M in all calls to can (M, K).

subtask	points	N	Q	<b>Additional Constraints</b>
1	21	$1 \le N \le 100$	$1 \leq Q \leq 100$	none
2	13	$1 \leq N \leq 100,000$	Q = 1	none
3	43	$1 \leq N \leq 100,000$	$1 \leq Q \leq 100,000$	$S \leq 100,000$
4	23	$1 \leq N \leq 500,000$	$1 \leq Q \leq 200,000$	$S \leq 200,000$

### Sample grader

The sample grader reads the input in the following format:

- line 1: N
- lines 2, ..., N + 1: A[i] B[i]
- line N + 2: Q
- lines N + 3, ..., N + Q + 2: M K[0] K[1] ... K[M 1]

For each question, the sample grader prints the return value of can.