



## Problem C. Cartesian MST

Input file:	standard input
Output file:	standard output
Time limit:	1 second
Memory limit:	512 mebibytes

Let G and H be two weighted undirected simple graphs. We define the *cartesian product* of the two graphs,  $G \Box H$ , as the graph whose vertex set is the cartesian set product of the vertex sets of the two graphs  $V(G) \times V(H)$  and in which there is an edge between vertices  $(u_1, v_1)$  and  $(u_2, v_2)$  if and only if:

- $v_1 = v_2$  and there is an edge  $(u_1, u_2)$  in G. In this case, the edge $((u_1, v_1), (u_2, v_2))$  in  $G \square H$  has the same weight as the edge  $(u_1, u_2)$  in G.
- or  $u_1 = u_2$  and there is an edge  $(v_1, v_2)$  in H. In this case, the edge $((u_1, v_1), (u_2, v_2))$  in  $G \Box H$  has the same weight as the edge  $(v_1, v_2)$  in H.

You are given two connected graphs G and H. Compute the total weight of the minimum spanning tree of  $G\Box H$ .

## Input

The first line contains four integers  $n_1, m_1, n_2, m_2$   $(2 \le n_1, n_2 \le 10^5; 1 \le m_1, m_2 \le 10^5)$ : the number of vertices of G, the number of edges of G, the number of vertices of H, and the number of edges of H, respectively.

Each of the next  $m_1$  lines contains three integers  $u_i, v_i, w_i$   $(0 \le u_i, v_i \le n_1 - 1; 1 \le w_i \le 10^8)$ , describing an edge of G between vertices  $u_i$  and  $v_i$  with weight  $w_i$ .

Each of the next  $m_2$  lines contains three integers  $u_i, v_i, w_i$   $(0 \le u_i, v_i \le n_2 - 1; 1 \le w_i \le 10^8)$ , describing an edge of H between vertices  $u_i$  and  $v_i$  with weight  $w_i$ .

It is guaranteed that graphs G and H are simple and connected. Recall that a graph is *simple* if there are no edges between a vertex and itself, and there is at most one edge between any two vertices.

## Output

Output one integer: the weight of the minimum spanning tree of  $G\Box H$ .

## Example

standard input	standard output
4 4 3 2	15
0 1 3	
1 2 2	
2 3 2	
3 0 5	
0 1 1	
1 2 1	