icpc $\begin{gathered}\text { university } \\ \text { commons }\end{gathered}$

## Problem H. Local Maxima

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
4 seconds
512 mebibytes

Given an $n \times m$ integer matrix $A$, a local maximum of $A$ is a location $(i, j)(1 \leq i \leq n$ and $1 \leq j \leq m)$ such that $A_{i, j}$ is no smaller than any other integer on the $i$-th row or on the $j$-th column.
For example, in the $3 \times 3$ matrix

$$
\left[\begin{array}{lll}
2 & 5 & 4 \\
2 & 1 & 6 \\
2 & 2 & 2
\end{array}\right],
$$

there are three local maxima: locations $(1,2),(2,3)$, and $(3,1)$ with values 5,6 , and 2 , repectively.
An $n \times m$ integer matrix $A$ is good if and only if it satisfies the following two conditions:

- There is exactly one local maximum in $A$.
- Each integer from 1 to $n \times m$ occurs exactly once in $A$.

Given $n, m$, and a prime number $P$, your task is to count the number of good matrices of size $n \times m$ modulo $P$.

## Input

The first line contains three integers, $n, m$, and $P$, where $1 \leq n, m \leq 3000$ and $10^{8} \leq P \leq 10^{9}+7$. It is guaranteed that $P$ is prime.

## Output

Output a single line with a single integer: the number of good matrices modulo $P$.

## Examples

| standard input | standard output |  |
| :--- | :--- | :--- |
| 221000000007 | 16 | 95800320 |
| 431000000007 | 848530760 |  |
| 100100998244353 |  |  |

