

## Problem I

### Encircling Circles

**Input:** Standard Input  
**Time Limit:** 30 seconds

You are given a set of circles  $C$  of a variety of radii (radiuses) placed at a variety of positions, possibly overlapping one another. Given a circle with radius  $r$ , that circle may be placed so that it encircles all of the circles in the set  $C$  if  $r$  is large enough.

There may be more than one possible position of the circle of radius  $r$  to encircle all the member circles of  $C$ . We define the region  $U$  as the union of the areas of encircling circles at all such positions. In other words, for each point in  $U$ , there exists a circle of radius  $r$  that encircles that point and all the members of  $C$ . Your task is to calculate the length of the periphery of that region  $U$ .

Figure I.1 shows an example of the set of circles  $C$  and the region  $U$ . In the figure, three circles contained in  $C$  are expressed by circles of solid circumference, some possible positions of the encircling circles are expressed by circles of dashed circumference, and the area  $U$  is expressed by a thick dashed closed curve.

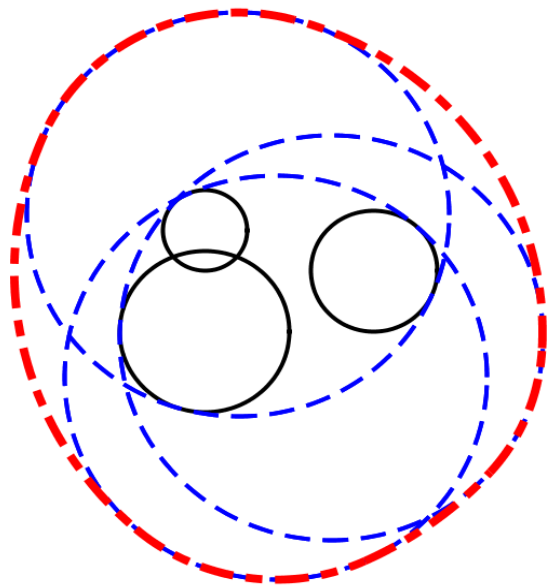


Figure I.1: Example of the Circle Set

## Input

The input is a sequence of datasets. The number of datasets is less than 100.

Each dataset is formatted as follows.

```
 $n$   $r$   
 $x_1$   $y_1$   $r_1$   
 $x_2$   $y_2$   $r_2$   
 $\vdots$   
 $x_n$   $y_n$   $r_n$ 
```

The first line of a dataset contains two positive integers,  $n$  and  $r$ , separated by a single space.  $n$  means the number of the circles in the set  $C$  and does not exceed 100.  $r$  means the radius of the encircling circle and does not exceed 1000.

Each of the  $n$  lines following the first line contains three integers separated by a single space.  $(x_i, y_i)$  means the center position of the  $i$ -th circle of the set  $C$  and  $r_i$  means its radius.

You may assume  $-500 \leq x_i \leq 500$ ,  $-500 \leq y_i \leq 500$ , and  $1 \leq r_i \leq 500$ .

The end of the input is indicated by a line containing two zeros separated by a single space.

## Output

For each dataset, output a line containing a decimal fraction which means the length of the periphery (circumferential length) of the region  $U$ .

The output should not contain an error greater than 0.01. You can assume that, when  $r$  changes by  $\epsilon$  ( $|\epsilon| < 0.0000001$ ), the length of the periphery of the region  $U$  will not change more than 0.001.

If  $r$  is too small to cover all of the circles in  $C$ , output a line containing only 0.0.

No other characters should be contained in the output.

## Sample Input

```
1 10  
5 5 7  
2 12  
5 5 7  
8 6 3  
3 10  
3 11 2
```

2 1 1  
2 16 3  
3 15  
-5 2 5  
9 2 9  
5 8 6  
3 38  
-25 -10 8  
30 5 7  
-3 35 11  
3 39  
-25 -10 8  
30 5 7  
-3 35 11  
3 800  
-400 400 2  
300 300 1  
300 302 1  
3 800  
400 -400 2  
300 300 1  
307 300 3  
8 147  
130 80 12  
130 -40 12  
-110 80 12  
-110 -40 12  
70 140 12  
70 -100 12  
-50 140 12  
-50 -100 12  
3 493  
345 154 10  
291 111 75  
-275 -301 46  
4 55  
54 0 1  
40 30 5  
27 36 10  
0 48 7  
3 30  
0 3 3  
-3 0 4  
400 0 3  
3 7  
2 3 2  
-5 -4 2

```

-4 3 2
3 10
-5 -4 5
2 3 5
-4 3 5
4 6
4 6 1
5 5 1
1 7 1
0 1 1
3 493
345 154 10
291 111 75
-275 -301 46
5 20
-9 12 5
0 15 5
3 -3 3
12 9 5
-12 9 5
0 0

```

### Output for the Sample Input

```

81.68140899333463
106.81415022205297
74.11215318612639
108.92086846105579
0.0
254.85616536128433
8576.936716409238
8569.462129048667
929.1977057481128
4181.124698202453
505.09134735536804
0.0
46.82023824234038
65.66979416387915
50.990642291793506
4181.124698202453
158.87951420768937

```

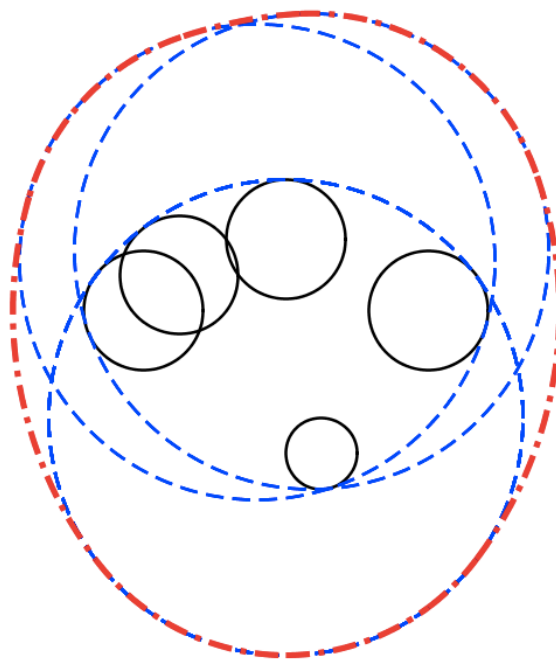


Figure I.2: Last Dataset of the Sample Input