

## Problem K – Kitten Greetings

Catarina loves all cats that live in her neighborhood. Her lifelong dream is to design a large cat-seeing circuit, so that every day she can go out and greet the cats while doing some exercise.

Catarina’s neighborhood can be represented as the 2D plane, with the North-South direction aligned with the  $y$ -axis. A cat-seeing circuit that visits  $m$  cats consists of exactly  $m$  steps. Catarina chooses a starting position  $(x_0, y_0)$  and faces one of the four cardinal directions. For each step  $i = 1, 2, \dots, m$  the following occurs:

- Catarina chooses a value  $k_i > 0$  and walks  $k_i$  units from  $(x_{i-1}, y_{i-1})$  straight ahead in her current direction, stopping at the location of a cat that she has not greeted during any previous step.
- Catarina greets the cat, taking some time to appreciate its beauty.
- Without turning around, Catarina walks another  $k_i$  units straight ahead in her current direction, stopping at a position  $(x_i, y_i)$ .
- Catarina turns  $90^\circ$  either clockwise or counterclockwise, facing again one of the four cardinal directions.

After completing all  $m$  steps, Catarina must be back to her starting position  $(x_0, y_0)$ , facing her initial direction. Notice that the length of the cat-seeing circuit is  $\sum_{i=1}^m 2k_i$ . When  $m = 0$ , the cat-seeing circuit has length 0.

Catarina knows the location of the  $N$  cats that live in her neighborhood. Surprisingly, no two cats have the same  $x$ -coordinate or the same  $y$ -coordinate. Your task is to determine the maximum length that a cat-seeing circuit can have.

### Input

The first line contains an integer  $N$  ( $1 \leq N \leq 4000$ ) indicating the number of cats.

Each of the next  $N$  lines describes a cat with two integers  $X$  and  $Y$  ( $-10^8 \leq X, Y \leq 10^8$ ), representing that the cat has coordinates  $(X, Y)$ .

No two cats have the same  $x$ -coordinate or  $y$ -coordinate (they differ in both of them).

### Output

Output a single line with an integer indicating the maximum length that a cat-seeing circuit can have.

#### Sample Input 1

```
5
1 2
2 1
0 0
-1 -2
-2 -1
```

#### Sample Output 1

```
0
```

#### Explanation of Sample 1:

In this case there is a circuit of length 16 that visits all the cats, but it is not a cat-seeing circuit because the cat at coordinates  $(0, 0)$  is greeted twice.

**Sample Input 2**

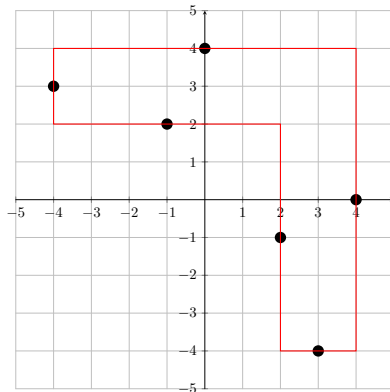
```
6
4 0
0 4
2 -1
-1 2
-4 3
3 -4
```

**Sample Output 2**

```
32
```

**Explanation of Sample 2:**

The picture below shows the location of the cats with small circles, together with a maximum-length cat-seeing circuit that visits all of them. The length of the circuit is 32.



**Sample Input 3**

```
7
2 1
0 -1
5 5
3 0
4 4
6 2
1 -2
```

**Sample Output 3**

```
24
```

**Explanation of Sample 3:**

It is possible to visit  $m = 6$  of the  $N = 7$  cats with a cat-seeing circuit of length 24.

