

Problem E

Parallel Sums

Time limit: 3 seconds

You are given two integers n and m . For a sequence of n integers $A = (a_1, a_2, \dots, a_n)$, the *parallel sums* of A are the $n - m + 1$ integers $s_1, s_2, \dots, s_{n-m+1}$ defined by $s_i = a_i + a_{i+1} + \dots + a_{i+m-1}$ for each i ($1 \leq i \leq n - m + 1$).

You are given the values of $s_1, s_2, \dots, s_{n-m+1}$. Your task is to answer q queries, described as follows. In the j -th query, you are given two integers l_j and r_j , and you are asked to find the smallest possible value of $\max(a_{l_j}, a_{l_j+1}, \dots, a_{r_j})$ among all sequences $A = (a_1, a_2, \dots, a_n)$ of n integers (possibly negative) such that $s_1, s_2, \dots, s_{n-m+1}$ are the parallel sums of A . Or determine if this value can be arbitrarily small.

Input

The first line of input contains two integers n and m ($1 \leq m \leq n \leq 200\,000$).

The second line contains $n - m + 1$ integers $s_1, s_2, \dots, s_{n-m+1}$ ($-10^9 \leq s_i \leq 10^9$).

The third line contains a single integer q ($1 \leq q \leq 100\,000$).

The j -th of the next q lines contains two integers l_j and r_j ($1 \leq l_j \leq r_j \leq n$).

Output

Output q lines. The j -th line should contain the smallest possible value of $\max(a_{l_j}, a_{l_j+1}, \dots, a_{r_j})$. If that value can be arbitrarily small, output unbounded instead.

Sample Input #1

```
8 4
4 -4 2 6 5
4
3 7
4 6
1 8
2 5
```

Sample Output #1

```
2
unbounded
4
-1
```

Explanation for the sample input/output #1

For the first query, take $A = (9, -4, -3, 2, 1, 2, 1, 1)$. The parallel sums of A are $(4, -4, 2, 6, 5)$ as required. Then $\max(a_3, \dots, a_7) = \max(-3, 2, 1, 2, 1) = 2$. It can be shown that 2 is the smallest possible value.

For the second query, you can make the value arbitrarily small.

For the third query, take $A = (4, -3, 0, 3, -4, 3, 4, 2)$. Then $\max(4, -3, 0, 3, -4, 3, 4, 2) = 4$, which is the smallest possible value.



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