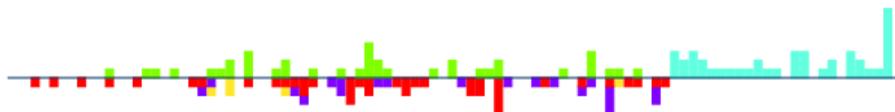


# D: Decelerating Jump

Problem Author: Onno Berrevoets

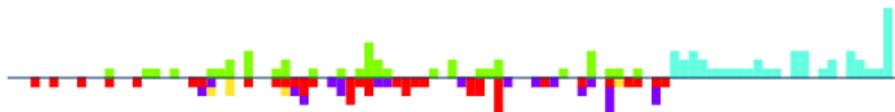


- **Problem:** Given a sequence of  $n$  integers  $p_1, \dots, p_n$ , find a subsequence  $1 = p_{i_1} < p_{i_2} < \dots < p_{i_k} = n$  such that the distance between consecutive elements does not increase.

Statistics: 146 submissions, 38 accepted, 43 unknown

# D: Decelerating Jump

Problem Author: Onno Berrevoets



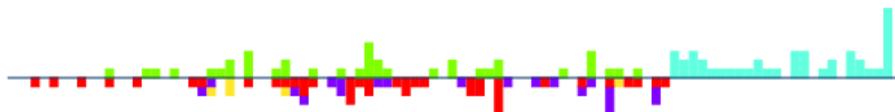
- **Problem:** Given a sequence of  $n$  integers  $p_1, \dots, p_n$ , find a subsequence  $1 = p_{i_1} < p_{i_2} < \dots < p_{i_k} = n$  such that the distance between consecutive elements does not increase.
- **Cubic solution:** Keep a DP table  $dp[\text{position}][\text{speed}]$ , which is computed as

$$dp[i][s] = p_i + \max_{k \geq s} dp[i - k][k]$$

Statistics: 146 submissions, 38 accepted, 43 unknown

# D: Decelerating Jump

Problem Author: Onno Berrevoets



- **Problem:** Given a sequence of  $n$  integers  $p_1, \dots, p_n$ , find a subsequence  $1 = p_{i_1} < p_{i_2} < \dots < p_{i_k} = n$  such that the distance between consecutive elements does not increase.
- **Cubic solution:** Keep a DP table  $dp[\text{position}][\text{speed}]$ , which is computed as

$$dp[i][s] = p_i + \max_{k \geq s} dp[i - k][k]$$

- **Quadratic solution:** Loop over speed  $s$  from  $n - 1$  to 1, keeping track of the maximum score if you end in each cell with speed at least  $s$ . Then update all positions  $i$  from 1 to  $n$ :

$$dp[i] = \max(dp[i], p_i + dp[i - s])$$

Statistics: 146 submissions, 38 accepted, 43 unknown