## Problem A. XOR Tree Path

Input file: standard input
Output file: standard output
Time limit: $\quad 2$ seconds
Memory limit: 1024 megabytes
You are given a rooted tree with $N$ vertices, labeled from 1 to $N$, where vertex 1 is the root. The $i$-th edge ( $1 \leq i \leq N-1$ ) connects vertices $U_{i}$ and $V_{i}$.
Each vertex of the tree is painted either white or black. Vertex $i(1 \leq i \leq N)$ is painted white if $A_{i}=0$, and black if $A_{i}=1$.
You can perform the following operation any number of times (possibly zero):

- Choose a leaf vertex $x$, and flip the color (change white vertices to black and black vertices to white) of all vertices on the path from the root to the vertex $x$ (including the root and the vertex $x)$.

Your goal is to maximize the number of black vertices. What is the maximum number of black vertices that can be achieved?

## Input

The input is given from Standard Input in the following format:

| $N$ |  |  |  |
| :--- | :--- | :--- | :--- |
| $A_{1}$ | $A_{2}$ | $\cdots$ | $A_{N}$ |
| $U_{1}$ | $V_{1}$ |  |  |
| $U_{2}$ | $V_{2}$ |  |  |
| $\vdots$ |  |  |  |
|  |  |  |  |
| $U_{N-1}$ | $V_{N-1}$ |  |  |

- All values in the input are integers.
- $2 \leq N \leq 10^{5}$
- $0 \leq A_{i} \leq 1(1 \leq i \leq N)$
- $1 \leq U_{i}, V_{i} \leq N(1 \leq i \leq N-1)$
- The given graph is a tree.


## Output

Output the maximum number of black vertices that can be achieved by performing any number of operations.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{llllll} \hline 5 & & & & \\ 1 & 0 & 0 & 1 & 0 \\ 1 & 2 & & & \\ 1 & 3 & & & \\ 3 & 4 & & & \\ 3 & 5 & & & \end{array}$ | $5$ |
| $\begin{array}{lllllll} 6 & & & & \\ 1 & 1 & 0 & 0 & 1 & 0 \\ 3 & 1 & & & & \\ 2 & 5 & & & & \\ 1 & 2 & & & & \\ 4 & 1 & & & & \\ 2 & 6 & & & & \end{array}$ | $5$ |
| $\begin{array}{\|lllllllllll} \hline 9 & & & & & & & & \\ 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 2 & 9 & & & & & & & \\ 1 & 2 & & & & & & & \\ 6 & 9 & & & & & & & & \\ 3 & 8 & & & & & & & & \\ 4 & 5 & & & & & & & \\ 5 & 9 & & & & & & & \\ 2 & 8 & & & & & & & \\ 7 & 8 & & & & & & & & \end{array}$ | $6$ |

## Note

In the first example, it is possible to make all vertices black by performing the following operations.

1. choose vertex 2 and perform the operation. This makes vertex 1 white and vertex 2 black.
2. choose vertex 5 and perform the operation. This makes vertex $1,3,5$ black.

## Problem B. Magical Wallet

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
2 seconds
1024 megabytes

You have a magical wallet with $X$ yen in it. (Yen is the currency of Japan.)
Using the magic on this wallet, you can rearrange the amount of money in the wallet as a decimal string in any order you like. For example, if you have a magical wallet with 120 yen, you can use magic to change the amount of money in the wallet to any of the following: 12 yen, 21 yen, 102 yen, 120 yen, 201 yen, or 210 yen (leading zeros are ignored).

You will now visit $N$ shops with the magical wallet in order. At the $i$-th shop $(1 \leq i \leq N)$, a product $\operatorname{costing} A_{i}$ yen is sold, and if the magical wallet contains at least $A_{i}$ yen, you can pay $A_{i}$ yen from the magical wallet to buy the product.

You can use magic as much as you like whenever you want. How many products can you buy at most?

## Input

The input is given from Standard Input in the following format:

| $N X$ |  |  |  |
| :--- | :--- | :--- | :--- |
| $A_{1}$ | $A_{2}$ | $\cdots$ | $A_{N}$ |

- All values in the input are integers.
- $1 \leq N \leq 100$
- $1 \leq X<10^{4}$
- $1 \leq A_{i}<10^{4}(1 \leq i \leq N)$


## Output

Print the answer.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{aligned} & 2120 \\ & 14290 \end{aligned}$ | 2 |
| $\begin{aligned} & 1119 \\ & 911 \end{aligned}$ | 1 |
| $\begin{aligned} & 51000 \\ & 900909009900 \end{aligned}$ | 3 |
| $\begin{array}{lllllll} 7 & 1171 \\ 6328 & 2419 & 8302 & 7503 & 1744 & 8495 & 1522 \end{array}$ | 5 |

## Note

In the first sample, you can buy two products by doing the following:

1. Use magic to change the amount of money in the wallet from 120 yen to 201 yen.
2. Buy a product for 142 yen at the first shop. The amount of money in the wallet becomes $201-142=59$ yen.
3. Use magic to change the amount of money in the wallet from 59 yen to 95 yen.
4. Buy a product for 90 yen at the second shop. The amount of money in the wallet becomes $95-90=5$ yen.

## Problem C. Parallel Processing (Easy)

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 2 seconds |
| Memory limit: | 1024 megabytes |

This is the easy version of the problem. The only difference between two versions is the constraint of $N$. You are given a mysterious monoid $(M, \oplus)$ and 4 CPUs to compute it.

Compute the cumulative $\oplus$ of a sequence $A=\left(A_{1}, A_{2}, \ldots, A_{N}\right)$ of $M$ in parallel using 4 CPUs, minimizing the number of operations.

## Statement

You are given an integer $N$. Write a program in a custom language to do the following and minimize the number of instructions in your program.

## Specification

This program can handle 2004 variables $A[1], A[2], \ldots, A[2000], C_{1}, C_{2}, C_{3}, C_{4}$. Each variable can hold a sequence of integers, and $A[i](1 \leq i \leq 2000)$ is initialized to $A[i]=(i)$. (Here $(i)$ denotes an integer sequence consisting of one $i$.)
At the end of the execution, the following condition must be satisfied:

- For each of $i=1,2, \ldots, N, A[i]=(1,2, \ldots, i)$ holds.


## Format

The first line of the program contains an integer $L$ representing the number of instructions in the program. The $L$ instructions are written in 4 lines per instruction from the 2 nd to the $(4 L+1)$-th lines, and are executed sequentially from top to bottom.

Each instruction is written as 12 integers $c_{1}, a_{1}, b_{1}, c_{2}, a_{2}, b_{2}, c_{3}, a_{3}, b_{3}, c_{4}, a_{4}, b_{4}$, where each integer must be between 1 and 2000 (inclusive).
For each instruction, the following operations are performed in order:

1. Assigns concat $\left(A\left[a_{1}\right], A\left[b_{1}\right]\right)$ to $C_{1}$.
2. Assigns concat $\left(A\left[a_{2}\right], A\left[b_{2}\right]\right)$ to $C_{2}$.
3. Assigns concat $\left(A\left[a_{3}\right], A\left[b_{3}\right]\right)$ to $C_{3}$.
4. Assigns concat $\left(A\left[a_{4}\right], A\left[b_{4}\right]\right)$ to $C_{4}$.
5. Assigns $C_{1}$ to $A\left[c_{1}\right]$.
6. Assigns $C_{2}$ to $A\left[c_{2}\right]$.
7. Assigns $C_{3}$ to $A\left[c_{3}\right]$.
8. Assigns $C_{4}$ to $A\left[c_{4}\right]$.

Here, concat $(x, y)$ denotes the sequence obtained by concatenating the sequences $x$ and $y$ in that order.

## Input

The input is given in the following format:

## N

- All values in the input are integers.
- $2 \leq N \leq 16$


## Output

Let $L$ be the minimum number of instructions. Output in the following format:

```
L
op
op}
\vdots
op
\[
\begin{array}{lll}
c_{1} & a_{1} & b_{1} \\
c_{2} & a_{2} & b_{2} \\
c_{3} & a_{3} & b_{3} \\
c_{4} & a_{4} & b_{4}
\end{array}
\]
```

$\mathrm{op}_{i}(1 \leq i \leq L)$ represents the $i$-th operation and should be output in the following format:

Here, each integer must be between 1 and 2000.

## Examples

| standard input | standard output |
| :---: | :---: |
| 2 | 1    <br> 2 1 2  <br> 2000 2000 2000  <br> 2000 2000 2000  <br> 2000 2000 2000  |
| 4 | 2    <br> 2 1 2  <br> 4 3 4  <br> 2000 2000 2000  <br> 2000 2000 2000  <br> 3 2 3  <br> 4 2 4  <br> 2000 2000 2000  <br> 2000 2000 2000  |

## Note

In the first example, the first operation changes $A[2]$ to $(1,2)$ and $A[2000]$ to $(2000,2000)$. At the end of the execution, $A[1]=(1)$ and $A[2]=(1,2)$, which satisfies the specification.

## Problem D. Parallel Processing (Hard)

Input file:
Output file:
Time limit:
Memory limit:
standard input standard output 2 seconds 1024 megabytes

This is the hard version of the problem. The only difference between two versions is the constraint of $N$. You are given a mysterious monoid $(M, \oplus)$ and 4 CPUs to compute it.
Compute the cumulative $\oplus$ of a sequence $A=\left(A_{1}, A_{2}, \ldots, A_{N}\right)$ of $M$ in parallel using 4 CPUs, minimizing the number of operations.

## Statement

You are given an integer $N$. Write a program in a custom language to do the following and minimize the number of instructions in your program.

## Specification

This program can handle 2004 variables $A[1], A[2], \ldots, A[2000], C_{1}, C_{2}, C_{3}, C_{4}$. Each variable can hold a sequence of integers, and $A[i](1 \leq i \leq 2000)$ is initialized to $A[i]=(i)$. (Here (i) denotes an integer sequence consisting of one $i$.)
At the end of the execution, the following condition must be satisfied:

- For each of $i=1,2, \ldots, N, A[i]=(1,2, \ldots, i)$ holds.


## Format

The first line of the program contains an integer $L$ representing the number of instructions in the program. The $L$ instructions are written in 4 lines per instruction from the 2 nd to the $(4 L+1)$-th lines, and are executed sequentially from top to bottom.
Each instruction is written as 12 integers $c_{1}, a_{1}, b_{1}, c_{2}, a_{2}, b_{2}, c_{3}, a_{3}, b_{3}, c_{4}, a_{4}, b_{4}$, where each integer must be between 1 and 2000 (inclusive).
For each instruction, the following operations are performed in order:

1. Assigns concat $\left(A\left[a_{1}\right], A\left[b_{1}\right]\right)$ to $C_{1}$.
2. Assigns concat $\left(A\left[a_{2}\right], A\left[b_{2}\right]\right)$ to $C_{2}$.
3. Assigns concat $\left(A\left[a_{3}\right], A\left[b_{3}\right]\right)$ to $C_{3}$.
4. Assigns concat $\left(A\left[a_{4}\right], A\left[b_{4}\right]\right)$ to $C_{4}$.
5. Assigns $C_{1}$ to $A\left[c_{1}\right]$.
6. Assigns $C_{2}$ to $A\left[c_{2}\right]$.
7. Assigns $C_{3}$ to $A\left[c_{3}\right]$.
8. Assigns $C_{4}$ to $A\left[c_{4}\right]$.

Here, concat $(x, y)$ denotes the sequence obtained by concatenating the sequences $x$ and $y$ in that order.

## Input

The input is given in the following format:

## N

- All values in the input are integers.
- $17 \leq N \leq 1000$


## Output

Let $L$ be the minimum number of instructions. Output in the following format:

```
L
op
op}
\vdots
op
```

$\mathrm{op}_{i}(1 \leq i \leq L)$ represents the $i$-th operation and should be output in the following format:

$$
\begin{array}{lll}
c_{1} & a_{1} & b_{1} \\
c_{2} & a_{2} & b_{2} \\
c_{3} & a_{3} & b_{3} \\
c_{4} & a_{4} & b_{4} \\
\hline
\end{array}
$$

Here, each integer must be between 1 and 2000.

## Problem E. Five Med Sum

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
2 seconds
1024 megabytes

You are given five integer sequences $A=\left(A_{1}, \ldots, A_{N}\right), B=\left(B_{1}, \ldots, B_{N}\right), C=\left(C_{1}, \ldots, C_{N}\right)$, $D=\left(D_{1}, \ldots, D_{N}\right)$, and $E=\left(E_{1}, \ldots, E_{N}\right)$ of length $N$.
Find the following value modulo 998244353.

$$
\sum_{i=1}^{N} \sum_{j=1}^{N} \sum_{k=1}^{N} \sum_{l=1}^{N} \sum_{m=1}^{N} \operatorname{med}\left(A_{i}, B_{j}, C_{k}, D_{l}, E_{m}\right)
$$

Here, $\operatorname{med}(a, b, c, d, e)$ represents the median of $a, b, c, d, e$.

## Input

The input is given from Standard Input in the following format:

| $N$ |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $A_{1}$ | $A_{2}$ | $\cdots$ | $A_{N}$ |
| $B_{1}$ | $B_{2}$ | $\cdots$ | $B_{N}$ |
| $C_{1}$ | $C_{2}$ | $\cdots$ | $C_{N}$ |
| $D_{1}$ | $D_{2}$ | $\cdots$ | $D_{N}$ |
| $E_{1}$ | $E_{2}$ | $\cdots$ | $E_{N}$ |

- All values in the input are integers.
- $1 \leq N \leq 10^{5}$
- $0 \leq A_{i}, B_{i}, C_{i}, D_{i}, E_{i}<998244353(1 \leq i \leq N)$


## Output

Print the answer.

## Examples

|  | standard input | standard output |
| :--- | :--- | :--- |
| 1 |  | 3 |
| 1 |  |  |
| 2 |  |  |
| 3 |  | 486 |
| 4 |  |  |
| 3 |  |  |
| 1 | 2 | 3 |
| 1 | 3 | 2 |
| 2 | 1 | 3 |
| 2 | 3 | 1 |

## Problem F. Forestry

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 4 seconds |
| Memory limit: | 1024 megabytes |

You are given a tree $T$ with $N$ vertices and $N-1$ edges. The vertices are numbered from 1 to $N$, and the edges are numbered from 1 to $N-1$. Edge $i(1 \leq i \leq N-1)$ connects vertices $U_{i}$ and $V_{i}$. Additionally, an integer $A_{v}$ is written on vertex $v(1 \leq v \leq N)$.
There are $2^{N-1}$ ways to choose some of the edges of the tree. For each choice, the score is defined as follows:

- Let $G$ be the graph obtained by removing the unselected edges from $T$. For each connected component of $G$, consider the minimum value of the integers written on its vertices, and sum those minimum values. The sum is the score.

Find the sum of the scores over all choices modulo 998244353.

## Input

The input is given from Standard Input in the following format:

```
N
A1 A 的利
U1 V
U2 V2
\vdots
UN-1}\mp@subsup{V}{N-1}{
```

- All values in the input are integers.
- $2 \leq N \leq 3 \times 10^{5}$
- $1 \leq A_{i} \leq 10^{9}(1 \leq i \leq N)$
- $1 \leq U_{i}, V_{i} \leq N(1 \leq i \leq N-1)$
- The given graph is a tree.


## Output

Output the answer.

## Examples

|  | standard input |  | standard output |
| :--- | :--- | :--- | :--- |
| 4 |  |  | 44 |
| 1 | 2 | 3 | 4 |
| 1 | 2 |  |  |
| 2 | 4 |  |  |
| 3 | 2 |  |  |
| 5 |  |  |  |
| 3 | 5 | 6 | 5 |
| 4 | 1 |  |  |
| 4 | 1 |  |  |
| 2 | 3 |  |  |
| 3 | 5 |  |  |
| 1 | 3 |  |  |

## Problem G. Range NEQ

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
2 seconds
1024 megabytes

You are given two positive integers $N$ and $M$.
Count the number of permutations $P=\left(P_{0}, P_{1}, \ldots, P_{N M-1}\right)$ of $(0,1, \ldots, N M-1)$ such that the following condition is satisfied, modulo 998244353.

- For all integers $i$ such that $0 \leq i<N M,\left\lfloor\frac{i}{M}\right\rfloor \neq\left\lfloor\frac{P_{i}}{M}\right\rfloor$ holds.


## Input

The input is given from Standard Input in the following format:

## N M

- All values in the input are integers.
- $2 \leq N \leq 1000$
- $1 \leq M \leq 1000$


## Output

Output the answer.

## Examples

| standard input | standard output |
| :--- | :--- |
| 22 | 4 |
| 51 | 44 |
| 16791 | 284830080 |

## Problem H. Expanded Hull

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
4 seconds
1024 megabytes

You are given integers $N, K$ and $N$ points $\left(X_{1}, Y_{1}, Z_{1}\right), \ldots,\left(X_{N}, Y_{N}, Z_{N}\right)$ in three-dimensional space.
Let $V$ be the convex hull of the $N$ points $\left(K X_{1}, K Y_{1}, K Z_{1}\right), \ldots,\left(K X_{N}, K Y_{N}, K Z_{N}\right)$. Count the number of points that are contained in the interior or on the boundary of $V$ and have integer coordinates, modulo 998244353.

## Input

The input is given from Standard Input in the following format:

```
N K
X1 Y1 Z1
\vdots
XN Y Y Z
```

- All values in the input are integers.
- $4 \leq N \leq 100$
- $1 \leq K \leq 10^{15}$
- $-200 \leq X_{i}, Y_{i}, Z_{i} \leq 200(1 \leq i \leq N)$
- $\left(X_{i}, Y_{i}, Z_{i}\right) \neq\left(X_{j}, Y_{j}, Z_{j}\right)(1 \leq i<j \leq N)$
- There is no plane passing through all $N$ points.


## Output

Output the answer.

## Examples



## Note

In the first example, there are 10 points that are contained in the interior or on the boundary of $V$ and have integer coordinates: $(0,0,0),(1,0,0),(2,0,0),(0,1,0),(1,1,0),(0,2,0),(0,0,1),(1,0,1),(0,1,1)$, $(0,0,2)$

## Problem I. Peaceful Results

Input file:
Output file
Time limit: 2 seconds
Memory limit:
standard input
standard output
1024 megabytes

Alice, Bob, and Chris will play rock-paper-scissors $N$ times. However, each of them has the following restrictions on what hand they can play:

- Alice must play rock exactly $A_{R}$ times, paper exactly $A_{P}$ times, and scissors exactly $A_{S}$ times.
- Bob must play rock exactly $B_{R}$ times, paper exactly $B_{P}$ times, and scissors exactly $B_{S}$ times.
- Chris must play rock exactly $C_{R}$ times, paper exactly $C_{P}$ times, and scissors exactly $C_{S}$ times.

Alice, Bob, and Chris are very good friends, so they want to make sure that they tie every single game over the $N$ rounds. Count the number of ways to choose the hands of the three players for the $N$ rounds that achieves this, modulo 998244353.

## Input

The input is given from Standard Input in the following format:

$$
\begin{array}{|lll}
\hline N \\
A_{R} & A_{P} & A_{S} \\
B_{R} & B_{P} & B_{S} \\
C_{R} & C_{P} & C_{S} \\
\hline
\end{array}
$$

- All values in the input are integers.
- $1 \leq N \leq 1.5 \times 10^{6}$
- $0 \leq A_{R}, A_{P}, A_{S}, B_{R}, B_{P}, B_{S}, C_{R}, C_{P}, C_{S} \leq 1.5 \times 10^{6}$
- $A_{R}+A_{P}+A_{S}=B_{R}+B_{P}+B_{S}=C_{R}+C_{P}+C_{S}=N$


## Output

Output the answer.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{lll} \hline 2 & & \\ 2 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 0 & 1 \end{array}$ | 2 |
| $\begin{array}{lll} 3 & & \\ 0 & 1 & 2 \\ 3 & 0 & 0 \\ 1 & 1 & 1 \end{array}$ | 0 |
| 333333   <br> 111111 111111 111111 <br> 111111 111111 111111 <br> 111111 111111 111111 | 383902959 |

## Problem J. Make Convex Sequence

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
2 seconds
1024 megabytes

You are given two integer sequences $L=\left(L_{1}, L_{2}, \ldots, L_{N}\right)$ and $R=\left(R_{1}, R_{2}, \ldots, R_{N}\right)$. Determine if there exists a sequence $A=\left(A_{1}, A_{2}, \ldots, A_{N}\right)$ of real numbers that satisfy the following conditions:

- For all integers $i$ such that $1 \leq i \leq N, L_{i} \leq A_{i} \leq R_{i}$ holds.
- For all integers $i$ such that $2 \leq i \leq N-1, A_{i-1}+A_{i+1} \geq 2 A_{i}$ holds.


## Input

The input is given from Standard Input in the following format:

| $N$ |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $L_{1}$ | $L_{2}$ | $\cdots$ | $L_{N}$ |
| $R_{1}$ | $R_{2}$ | $\cdots$ | $R_{N}$ |

- All values in the input are integers.
- $3 \leq N \leq 3 \times 10^{5}$
- $1 \leq L_{i} \leq R_{i} \leq 10^{9}(1 \leq i \leq N)$


## Output

If there exists a sequence $A$ of real numbers that satisfies the conditions, output Yes. Otherwise, output No.

## Examples

|  |  |  | standard input |  | standard output |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 4 |  |  | Yes |  |  |
| 2 | 1 | 2 | 5 |  |  |
| 4 | 6 | 5 | 8 |  | No |
| 3 |  |  |  |  |  |
| 1 | 4 | 2 |  |  |  |
| 3 | 7 | 4 |  |  |  |

## Note

In the first example, for example, $A=\left(4, \frac{3}{2}, 3,7\right)$ satisfies the conditions.

## Problem K. Count Arithmetic Progression

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
2 seconds
1024 megabytes

You are given two sequences of integers $L=\left(L_{1}, L_{2}, \ldots, L_{N}\right)$ and $R=\left(R_{1}, R_{2}, \ldots, R_{N}\right)$, find the number of sequences $A=\left(A_{1}, A_{2}, \ldots, A_{N}\right)$ of integers that satisfy the following conditions, modulo 998244353:

- For all integers $i$ such that $1 \leq i \leq N, L_{i} \leq A_{i} \leq R_{i}$ holds.
- Let $d=A_{2}-A_{1}$. For all integers $i$ such that $1 \leq i \leq N-1, A_{i+1}-A_{i}=d$ holds.


## Input

The input is given from Standard Input in the following format:

```
N
L_ L L2\cdots L
R1 R2\cdots 语
```

- All values in the input are integers.
- $2 \leq N \leq 3 \times 10^{5}$
- $1 \leq L_{i} \leq R_{i} \leq 10^{12}(1 \leq i \leq N)$


## Output

Print the number of sequences $A$ that satisfy the conditions, modulo 998244353 .

## Examples

|  | standard input | standard output |  |
| :--- | :--- | :--- | :--- |
| 3 |  |  | 6 |
| 5 | 5 | 2 |  |
| 7 | 6 | 7 |  |
| 4 |  |  | 0 |
| 2 | 3 | 1 | 6 |
| 5 | 6 | 4 | 8 |

## Note

In the first example, there are 6 sequences that satisfy the conditions: $(5,5,5),(5,6,7),(6,5,4),(6,6,6)$, $(7,5,3),(7,6,5)$.

## Problem L. Many Products

Input file:
standard input
Output file: standard output
Time limit:
Memory limit:
1024 megabytes
You are given two positive integers $N$ and $M$ and a sequence of integers $A=\left(A_{1}, A_{2}, \ldots, A_{N}\right)$. Let $\boldsymbol{X}$ be the set of all $N$-tuples of positive integers $\left(x_{1}, x_{2}, \ldots, x_{N}\right)$ that satisfy $\left(\prod_{i=1}^{N} x_{i}\right)=M$.
Find the following value modulo 998244353.

$$
\sum_{\left(x_{1}, x_{2}, \ldots, x_{N}\right) \in \boldsymbol{X}} \prod_{i=1}^{N}\left(x_{i}+A_{i}\right)
$$

## Input

The input is given from Standard Input in the following format:

| $N M$ |  |  |
| :--- | :--- | :--- |
| $A_{1}$ | $A_{2}$ | $\cdots$ |$A_{N}$

- All values in the input are integers.
- $1 \leq N \leq 2 \times 10^{5}$
- $1 \leq M \leq 10^{12}$
- $0 \leq A_{i}<998244353(1 \leq i \leq N)$


## Output

Output the answer.

## Examples

|  | standard input | standard output |
| :--- | :--- | :--- |
| 2 | 3 |  |
| 0 | 1 |  |
| 5 | 1 |  |
| 0 | 1 | 2 |
| 5 | 4 | 120 |
| 10314159265358 |  |  |
| 0 | 1 | 2 |
| 3 | 456789 | 6 |

## Note

In the first sample, $\boldsymbol{X}=\{(1,3),(3,1)\}$, and the answer is $(1+0)(3+1)+(3+0)(1+1)=10$.

## Problem M. Colorful Graph

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
8 seconds
64 megabytes

You are given a directed graph with $N$ vertices and $M$ edges. The vertices are numbered from 1 to $N$, and the edges are numbered from 1 to $M$. Edge $i(1 \leq i \leq M)$ goes from vertex $A_{i}$ to vertex $B_{i}$.
Your task is to color each vertex of the graph with one of the colors $1, \ldots, N$ in such a way that the following conditions are satisfied:

- For each vertex $i(1 \leq i \leq N)$, let $c_{i}$ be the color assigned to it. For any pair $(i, j)(1 \leq i<j \leq N)$ such that $c_{i}=c_{j}$, there exists a path from vertex $i$ to vertex $j$ or from vertex $j$ to vertex $i$ (or both).
- The value of $\max \left\{c_{1}, \ldots, c_{N}\right\}$ is as small as possible.

Construct one coloring that satisfies these conditions.

## Input

The input is given from Standard Input in the following format:

|  $M$ <br> $A_{1}$ $B_{1}$ <br> $A_{2}$ $B_{2}$ <br> $\vdots$  <br> $A_{M}$ $B_{M}$ |
| :--- | :--- | :--- |

- All values in the input are integers.
- $1 \leq N \leq 7 \times 10^{3}$
- $0 \leq M \leq 7 \times 10^{3}$
- $1 \leq A_{i}, B_{i} \leq N(1 \leq i \leq M)$
- $A_{i} \neq B_{i}(1 \leq i \leq M)$
- $\left(A_{i}, B_{i}\right) \neq\left(A_{j}, B_{j}\right)(1 \leq i<j \leq M)$


## Output

Output the color assignment $c_{1}, c_{2}, \ldots, c_{N}$ that satisfies these conditions.

## Examples

| standard input | standard output |
| :---: | :---: |
| 5 5 <br> 1 4 <br> 2 3 <br> 1 3 <br> 2 5 <br> 5 1 | 21122 |
| $\begin{array}{ll} 5 & 7 \\ 1 & 2 \\ 2 & 1 \\ 4 & 3 \\ 5 & 1 \\ 5 & 4 \\ 4 & 1 \\ 4 & 5 \end{array}$ | 22111 |
| 8 6 <br> 6 1 <br> 3 4 <br> 3 6 <br> 2 3 <br> 4 1 <br> 6 4 | 44443421 |

## Note

The memory limit for this problem is 64 MB .

## Problem N. XOR Reachable

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 3 seconds |
| Memory limit: | 1024 megabytes |

You are given integers $N, M$, and $K$, and an undirected graph with $N$ vertices and $M$ edges. The vertices are numbered from 1 to $N$, and the edges are numbered from 1 to $M$. Edge $i(1 \leq i \leq M)$ connects vertices $A_{i}$ and $B_{i}$, and has a non-negative integer weight $C_{i}$. The graph may have multiple edges, but there are no self-loops.

You are given $Q$ queries. In the $i$-th $(1 \leq i \leq Q)$ query, you are given an integer $D_{i}$. Find the number of pairs of integers $(u, v)$ that satisfy the following conditions:

- $1 \leq u<v \leq N$
- It is possible to move from vertex $u$ to vertex $v$ by only using edges $j$ such that $\left(C_{j} \oplus D_{i}\right)<K$, where $\oplus$ denotes the bitwise XOR operation.


## Input

The input is given from Standard Input in the following format:

```
N M K
\(A_{1} B_{1} C_{1}\)
\(A_{2} B_{2} C_{2}\)
\(A_{M} B_{M} C_{M}\)
\(Q\)
\(D_{1}\)
\(D_{2}\)
\(\vdots\)
\(D_{Q}\)
```

- All values in the input are integers.
- $2 \leq N \leq 10^{5}$
- $1 \leq M \leq 10^{5}$
- $0 \leq K<2^{30}$
- $1 \leq A_{i}<B_{i} \leq N(1 \leq i \leq M)$
- $0 \leq C_{i}<2^{30}(1 \leq i \leq M)$
- $1 \leq Q \leq 10^{5}$
- $0 \leq D_{i}<2^{30}(1 \leq i \leq Q)$


## Output

Output $Q$ lines. The $i$-th line should contain the answer to the $i$-th query.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{lll} 4 & 5 & 5 \\ 1 & 2 & 17 \\ 1 & 3 & 4 \\ 2 & 3 & 20 \\ 2 & 4 & 3 \\ 3 & 4 & 5 \\ 4 & & \\ 0 & & \\ 7 & & \\ 16 & & \\ 167 & \end{array}$ | $\begin{aligned} & 2 \\ & 6 \\ & 3 \\ & 0 \end{aligned}$ |
| 9 13 488888932 <br> 2 7 771479959 <br> 3 8 783850182 <br> 5 7 430673756 <br> 6 8 350738034 <br> 4 9 400768807 <br> 2 3 83653266 <br> 1 2 829786563 <br> 5 8 357613791 <br> 7 9 579696618 <br> 3 7 423191200 <br> 3 5 867380255 <br> 1 9 907715012 <br> 6 9 1033650694 <br> 8   <br> 498260055   <br> 144262908   <br> 117665696   <br> 848664012   <br> 983408133   <br> 32610599   <br> 478007408   <br> 134182829   | 16 7 5 13 13 16 16 5 |

## Problem O. Jewel Game

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 3 seconds |
| Memory limit: | 1024 megabytes |

You are given a directed graph with $N$ vertices and $M$ edges. The vertices are numbered from 1 to $N$, and the edges are numbered from 1 to $M$. Edge $i(1 \leq i \leq M)$ goes from vertex $U_{i}$ to vertex $V_{i}$. The graph may have self-loops, but there are no multiple edges. It is guaranteed that there is at least one edge going out from each vertex.

There are $K$ jewels placed on some of the vertices. The $i$-th $(1 \leq i \leq K)$ jewel is located at vertex $X_{i}$ and has value $W_{i}$.
Alice and Bob are playing a game using this graph. At the beginning of the game, Alice is at vertex $A$, and Bob is at vertex $B$. Starting with Alice, Alice and Bob take turns performing the following action:

- Choose one edge going out from the vertex they are currently on and move to the next vertex along that edge. If the next vertex has a jewel, they take the jewel and remove it from the graph.

The game ends when either all jewels are taken, or the current state of the game (turn, positions of both players, remaining jewels) has appeared before. At the end of the game, the score of the game is defined as:
(the sum of the values of the gems taken by Alice) - (the sum of the values of the gems taken by Bob)
Alice wants to maximize this score, while Bob wants to minimize it. Find the score of the game when both players play optimally.

## Input

The input is given from Standard Input in the following format:

```
N M A B
U1 V1
\vdots
UM VM
K
X1 W1
:
XK}\mp@subsup{W}{K}{
```

- All values in the input are integers.
- $2 \leq N \leq 30$
- $1 \leq A, B \leq N$
- $1 \leq U_{i}, V_{i} \leq N(1 \leq i \leq M)$
- $\left(U_{i}, V_{i}\right) \neq\left(U_{j}, V_{j}\right)(1 \leq i<j \leq M)$
- For every $x(1 \leq x \leq N)$, there exists at least one $i$ such that $U_{i}=x$.
- $1 \leq K \leq 10$
- $1 \leq X_{1}<\cdots<X_{K} \leq N$
- $X_{i} \notin\{A, B\}(1 \leq i \leq K)$
- $1 \leq W_{i} \leq 10^{8}(1 \leq i \leq K)$


## Output

Print the score of the game when both players play optimally.

## Examples

| standard input | standard output |
| :---: | :---: |
|  | $46$ |
| 8 16 8 4 <br> 1 2   <br> 2 3   <br> 3 4   <br> 4 5   <br> 5 6   <br> 6 7   <br> 7 8   <br> 8 1   <br> 1 5   <br> 2 6   <br> 3 7   <br> 4 8   <br> 5 1   <br> 6 2   <br> 7 3   <br> 8 4   <br> 6    <br> 1 29   <br> 2 34   <br> 3 41   <br> 5 7   <br> 6 26   <br> 7 94   | $-23$ |

