

## Problem A. Maximum Multiple

Input file: *standard input*  
Output file: *standard output*  
Time limit: 2 seconds  
Memory limit: 256 mebibytes

Given an integer  $n$ , Chiaki would like to find three positive integers  $x$ ,  $y$  and  $z$  such that:  $n = x + y + z$ ,  $x \mid n$ ,  $y \mid n$ ,  $z \mid n$  and  $xyz$  is maximum.

### Input

There are multiple test cases. The first line of input contains an integer  $T$  ( $1 \leq T \leq 10^6$ ), indicating the number of test cases. For each test case:

The first line contains an integer  $n$  ( $1 \leq n \leq 10^6$ ).

### Output

For each test case, output an integer denoting the maximum  $xyz$ . If there no such integers, output  $-1$  instead.

### Example

standard input	standard output
3	-1
1	-1
2	1
3	

## Problem B. Balanced Sequence

Input file: *standard input*  
 Output file: *standard output*  
 Time limit: 1 second  
 Memory limit: 256 mebibytes

Chiaki has  $n$  strings  $s_1, s_2, \dots, s_n$  consisting of '(' and ')'. A string of this type is said to be *balanced*:

- if it is the empty string
- if  $A$  and  $B$  are balanced,  $AB$  is balanced,
- if  $A$  is balanced,  $(A)$  is balanced.

Chiaki can reorder the strings and then concatenate them get a new string  $t$ . Let  $f(t)$  be the length of the longest balanced subsequence (not necessary continuous) of  $t$ . Chiaki would like to know the maximum value of  $f(t)$  for all possible  $t$ .

### Input

There are multiple test cases. The first line of input contains an integer  $T$ , indicating the number of test cases. For each test case:

The first line contains an integer  $n$  ( $1 \leq n \leq 10^5$ ) – the number of strings.

Each of the next  $n$  lines contains a string  $s_i$  ( $1 \leq |s_i| \leq 10^5$ ) consisting of '(' and ')'. It is guaranteed that the sum of all  $|s_i|$  does not exceeds  $5 \times 10^6$ .

### Output

For each test case, output an integer denoting the answer.

### Example

standard input	standard output
2	4
1	2
)()() (	
2	
)	
) (	

## Problem C. Triangle Partition

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 256 mebibytes

Chiaki has  $3n$  points  $p_1, p_2, \dots, p_{3n}$ . It is guaranteed that no three points are collinear.

Chiaki would like to construct  $n$  disjoint triangles where each vertex comes from the  $3n$  points.

### Input

There are multiple test cases. The first line of input contains an integer  $T$ , indicating the number of test cases. For each test case:

The first line contains an integer  $n$  ( $1 \leq n \leq 1000$ ) – the number of triangle to construct.

Each of the next  $3n$  lines contains two integers  $x_i$  and  $y_i$  ( $-10^9 \leq x_i, y_i \leq 10^9$ ).

It is guaranteed that the sum of all  $n$  does not exceed  $10^4$ .

### Output

For each test case, output  $n$  lines contain three integers  $a_i, b_i, c_i$  ( $1 \leq a_i, b_i, c_i \leq 3n$ ) each denoting the indices of points the  $i$ -th triangle use. If there are multiple solutions, you can output any of them.

### Example

standard input	standard output
1 1 1 2 2 3 3 5	1 2 3

## Problem D. Distinct Values

Input file: *standard input*  
 Output file: *standard output*  
 Time limit: 2 seconds  
 Memory limit: 256 mebibytes

Chiaki has an array of  $n$  positive integers. You are told some facts about the array: for every two elements  $a_i$  and  $a_j$  in the subarray  $a_{l..r}$  ( $l \leq i < j \leq r$ ),  $a_i \neq a_j$  holds.

Chiaki would like to find a lexicographically minimal array which meets the facts.

### Input

There are multiple test cases. The first line of input contains an integer  $T$ , indicating the number of test cases. For each test case:

The first line contains two integers  $n$  and  $m$  ( $1 \leq n, m \leq 10^5$ ) – the length of the array and the number of facts. Each of the next  $m$  lines contains two integers  $l_i$  and  $r_i$  ( $1 \leq l_i \leq r_i \leq n$ ).

It is guaranteed that neither the sum of all  $n$  nor the sum of all  $m$  exceeds  $10^6$ .

### Output

For each test case, output  $n$  integers denoting the lexicographically minimal array. Integers should be separated by a single space, and no extra spaces are allowed at the end of lines.

### Example

standard input	standard output
3	1 2
2 1	1 2 1 2
1 2	1 2 3 1 1
4 2	
1 2	
3 4	
5 2	
1 3	
2 4	

## Problem E. Maximum Weighted Matching

Input file: *standard input*  
Output file: *standard output*  
Time limit: 4 seconds  
Memory limit: 256 mebibytes

Chiaki is good at generating special graphs. Initially, she has a graph with only two vertices connected by an edge. Each time, she can choose an edge  $(u, v)$ , make a copy of it, insert some new vertices (maybe zero) in the edge (i.e. let the new vertices be  $t_1, t_2, \dots, t_k$ , Chiaki would insert edges  $(u, t_1)$ ,  $(t_1, t_2)$ ,  $\dots, (t_{k-1}, t_k)$ ,  $(t_k, v)$  into the graph).

Given a weighted graph generated by above operations, Chiaki would like to know the maximum weighted matching of the graph and the number different maximum weighted matchings modulo  $(10^9 + 7)$ .

A matching in a graph is a set of pairwise non-adjacent edges, none of which are loops; that is, no two edges share a common vertex.

A maximum weighted matching is defined as a matching where the sum of the values of the edges in the matching have a maximal value.

### Input

There are multiple test cases. The first line of input contains an integer  $T$ , indicating the number of test cases. For each test case:

The first line contains two integers  $n$  and  $m$  ( $1 \leq n, m \leq 10^5$ ) – the number of vertices and the number of edges.

Each of the next  $m$  lines contains three integers  $u_i$ ,  $v_i$  and  $w_i$  ( $1 \leq u_i, v_i \leq n, 1 \leq w_i \leq 10^9$ ) – denoting an edge between  $u_i$  and  $v_i$  with weight  $w_i$ .

It is guaranteed that neither the sum of all  $n$  nor the sum of all  $m$  exceeds  $10^6$ .

### Output

For each test case, output two integers separated by a single space. The first one is the sum of weight and the second one is the number of different maximum weighted matchings modulo  $(10^9 + 7)$ .

### Example

standard input	standard output
2	3 3
6 7	2 2
1 2 1	
2 3 1	
4 5 1	
5 6 1	
1 4 1	
2 5 1	
3 6 1	
4 5	
1 2 1	
1 3 1	
1 4 1	
2 3 1	
3 4 1	

## Problem F. Period Sequence

Input file: *standard input*  
Output file: *standard output*  
Time limit: 6 seconds  
Memory limit: 256 mebibytes

Chiaki has  $n$  integers  $s_0, s_1, \dots, s_{n-1}$ . She has defined an infinite sequence  $S$  in the following way:  $S_k = s_{k \bmod n} + n \cdot \lfloor \frac{k}{n} \rfloor$ , where  $k$  is a zero based index.

For a continuous subsequence  $S[l..r]$ , let  $cnt_x$  be the number of occurrence of  $x$  in the subsequence  $S[l..r]$ . Then the value of  $S[l..r]$  is defined as follows

$$f(l, r) = \sum_x x \cdot cnt_x^2$$

For two integers  $a$  and  $b$  ( $a \leq b$ ), Chiaki would like to find the value of

$$(\sum_{a \leq l \leq r \leq b} f(l, r)) \bmod (10^9 + 7)$$

### Input

There are multiple test cases. The first line of input contains an integer  $T$ , indicating the number of test cases. For each test case:

The first line contains three integers  $n$ ,  $a$  and  $b$  ( $1 \leq n \leq 2000, 0 \leq a \leq b \leq 10^{18}$ ).

The second line contains  $n$  integers  $s_0, s_1, \dots, s_{n-1}$  ( $0 \leq s_i \leq 10^9$ ).

It is guaranteed that the sum of all  $n$  does not exceed  $2 \cdot 10^4$ .

### Output

For each test case, output an integer denoting the answer.

### Example

standard input	standard output
4	179
3 2 6	268
2 1 3	369
5 2 7	437
2 1 5 1 2	
4 4 8	
2 1 5 17	
3 5 9	
2 5 2	

## Problem G. Chiaki Sequence Revisited

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 256 mebibytes

Chiaki is interested in an infinite sequence  $a_1, a_2, a_3, \dots$ , which is defined as follows:

$$a_n = \begin{cases} 1 & n = 1, 2 \\ a_{n-a_{n-1}} + a_{n-1-a_{n-2}} & n \geq 3 \end{cases}$$

Chiaki would like to know the sum of the first  $n$  terms of the sequence, i.e.  $\sum_{i=1}^n a_i$ . As this number may be very large, Chiaki is only interested in its remainder modulo  $(10^9 + 7)$ .

### Input

There are multiple test cases. The first line of input contains an integer  $T$  ( $1 \leq T \leq 10^5$ ), indicating the number of test cases. For each test case:

The first line contains an integer  $n$  ( $1 \leq n \leq 10^{18}$ ).

### Output

For each test case, output an integer denoting the answer.

### Example

standard input	standard output
10	1
1	2
2	4
3	6
4	9
5	13
6	17
7	21
8	26
9	32
10	

## Problem H. RMQ Similar Sequence

Input file: *standard input*  
 Output file: *standard output*  
 Time limit: 2 seconds  
 Memory limit: 256 mebibytes

Chiaki has a sequence  $A = \{a_1, a_2, \dots, a_n\}$ . Let  $\mathbf{RMQ}(A, l, r)$  be the minimum  $i$  ( $l \leq i \leq r$ ) such that  $a_i$  is the maximum value in  $a_l, a_{l+1}, \dots, a_r$ .

Two sequences  $A$  and  $B$  are called *RMQ Similar*, if they have the same length  $n$  and for every  $1 \leq l \leq r \leq n$ ,  $\mathbf{RMQ}(A, l, r) = \mathbf{RMQ}(B, l, r)$ .

For a given the sequence  $A = \{a_1, a_2, \dots, a_n\}$ , define the weight of a sequence  $B = \{b_1, b_2, \dots, b_n\}$  be  $\sum_{i=1}^n b_i$  (i.e. the sum of all elements in  $B$ ) if sequence  $B$  and sequence  $A$  are RMQ Similar, or 0 otherwise.

If each element of  $B$  is a real number chosen independently and uniformly at random between 0 and 1, find the expected weight of  $B$ .

### Input

There are multiple test cases. The first line of input contains an integer  $T$ , indicating the number of test cases. For each test case:

The first line contains an integer  $n$  ( $1 \leq n \leq 10^6$ ) – the length of the sequence.

The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq n$ ) denoting the sequence.

It is guaranteed that the sum of all  $n$  does not exceed  $3 \times 10^6$ .

### Output

For each test case, output the answer as a value of a rational number modulo  $10^9 + 7$ .

Formally, it is guaranteed that under given constraints the probability is always a rational number  $\frac{p}{q}$  ( $p$  and  $q$  are integer and coprime,  $q$  is positive), such that  $q$  is not divisible by  $10^9 + 7$ . Output such integer  $a$  between 0 and  $10^9 + 6$  that  $p - aq$  is divisible by  $10^9 + 7$ .

### Example

standard input	standard output
3	250000002
3	500000004
1 2 3	125000001
3	
1 2 1	
5	
1 2 3 2 1	



## Problem I. Lyndon Substring

Input file: *standard input*  
Output file: *standard output*  
Time limit: 3 seconds  
Memory limit: 256 mebibytes

A string  $w$  is said to be a Lyndon word if  $w$  is lexicographically smaller than any of its cyclic rotations.

The longest Lyndon substring of a string  $s$  is the longest substring of  $s$  which is a Lyndon word.

Chiaki has  $n$  strings  $s_1, s_2, \dots, s_n$ . She has some queries: for some pair  $(i, j)$ , find the length of the longest Lyndon substring of string  $s_i s_j$ .

### Input

There are multiple test cases. The first line of input contains an integer  $T$ , indicating the number of test cases. For each test case:

The first line contains two integers  $n$  and  $m$  ( $1 \leq n, m \leq 10^5$ ) – the number of strings and the number of queries.

Each of the next  $n$  lines contains a nonempty string  $s_i$  ( $1 \leq s_i \leq 10^5$ ) consisting of lowercase English letters.

Each of the next  $m$  lines contains two integers  $i$  and  $j$  ( $1 \leq i, j \leq n$ ) denoting a query.

It is guaranteed that in one test case the sum of all  $|s|$  does not exceed  $5 \times 10^5$  and that in all cases the sum of all  $|s|$  does not exceed  $5 \times 10^6$ .

It is guaranteed that neither the sum of all  $n$  nor the sum of all  $m$  exceeds  $10^6$ .

### Output

For each query, output an integer denoting the answer.

### Example

standard input	standard output
1 2 1 aa bb 1 2	4

## Problem J. Turn Off The Light

Input file: *standard input*  
Output file: *standard output*  
Time limit: 2 seconds  
Memory limit: 256 mebibytes

There are  $n$  lights aligned in a row. These lights are numbered 1 to  $n$  from left to right. Initially some of the lights are turned on. Chiaki would like to turn off all the lights.

Chiaki starts from the  $p$ -th light. Each time she can go left or right (i.e. if Chiaki is at  $x$ , then she can go to  $x - 1$  or  $x + 1$ ) and then press the switch of the light in that position (i.e. if the light is turned on before, it will be turned off and vice versa).

For each  $p = 1, 2, \dots, n$ , Chiaki would like to know the minimum steps needed to turn off all the lights.

### Input

There are multiple test cases. The first line of input is an integer  $T$  indicates the number of test cases. For each test case:

The first line contains an integer  $n$  ( $2 \leq n \leq 10^6$ ) – the number of lights.

The second line contains a binary string  $s$  where  $s_i = 1$  means the  $i$ -th light is turned on and  $s_i = 0$  means  $i$ -th light is turned off.

It is guaranteed that the sum of all  $n$  does not exceed  $10^7$ .

### Output

For each test cases, output  $(\sum_{i=1}^{|s|} i \times z_i) \bmod (10^9 + 7)$ , where  $z_i$  is the number of step needed when Chikai starts at the  $i$ -th light.

### Example

standard input	standard output
3	0
3	26
000	432
3	
111	
8	
01010101	

## Problem K. Time Zone

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1 second  
Memory limit: 256 mebibytes

Chiaki often participates in international competitive programming contests. The time zone becomes a big problem.

Given a time in Beijing time (UTC +8), Chiaki would like to know the time in another time zone  $s$ .

### Input

There are multiple test cases. The first line of input contains an integer  $T$  ( $1 \leq T \leq 10^5$ ), indicating the number of test cases. For each test case:

The first line contains two integers  $a, b$  ( $0 \leq a \leq 23, 0 \leq b \leq 59$ ) and a string  $s$  in the format of “UTC+ $X$ ”, “UTC- $X$ ”, “UTC+ $X.Y$ ”, or “UTC- $X.Y$ ” ( $0 \leq X, X.Y \leq 14$ ).

### Output

For each test, output the time in the format of  $hh:mm$  (24-hour clock).

### Example

standard input	standard output
3	11:11
11 11 UTC+8	12:12
11 12 UTC+9	03:23
11 23 UTC+0	