
? $\cap$ International Collegiate Programming Contest

# UIUC ICPC Spring Coding Contest 

Saturday, April 13th, 2019

## Contest Overview

DO NOT turn this page until instructed to do so. Contest runs from 12 pm to 5 pm .
There are 11 problems in total, not ordered from easiest to hardest. However, the problems are weighted the same regardless of difficulty, so find easy problems and solve them first!

Teams are ranked by the number of problems they solve; ties are broken by cumulated time penalty.

Each team will be assigned one EWS workstation to work on, so your team members cannot code simultaneously. Allocate your time wisely! When one person is coding, others can solve problems on paper, or look at some code on the other screen. (Sorry but no printing service is provided)

Online judge: login to $\underline{h t t p: / / d o m j u d g e 2 . c s . i l l i n o i s . e d u / t e a m / ~ w i t h ~ c r e d e n t i a l s ~ s e n t ~ t o ~ y o u r ~ e m a i l . ~}$
Allowed digital reference materials are linked at http://icpc.cs.illinois.edu/scc.html. All other digital materials (Google, Stack Overflow, etc.) are strictly forbidden. Any physical materials (books, notes, printed code, etc.) are allowed.

If you have any questions, please raise your hand. Our officers will be there to help you.

## Problem A. AK the Problems

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 2 seconds |
| Memory limit: | 256 MB |

Suzukaze, a Codefalser who has the master title, is now competing in a contest on Codefalses. He has solved all the problems except the last one and there are only ten minutes left. This is a crucial contest to Suzukaze so he is asking for your help. The problem statement follows:

Two players are given a forest(undirected acyclic graph) and decide to play a game on it. The first player plays first and they take alternating turns. In each turn, the current player can either 1) delete an edge or 2 ) delete a vertex and the edges on it. Whoever is unable to make a move, loses. Determine who wins if they both play optimally.

If Suzukaze solves this last problem and AK the problemset, he will achieve a new title - grandmaster . However, if he fails on this problem, he will lose all the ratings and stop competing in any contests. Can you help him solve this problem?

## Input

The first line contains two integers $n$ and $m\left(1 \leq n \leq 10^{5}, 0 \leq m \leq n-1\right)$, the number of vertices in the forest and the number of edges in the forest. The vertices in the forest are labeled from 1 to $n$.

In the following $m$ lines, each of the lines contains 2 integers $u, v(1 \leq u, v \leq n ; u \neq v)$, which means that there is an undirected edge connecting vertex $u$ and vertex $v$.
It's guaranteed that the input data is a forest.

## Output

If the first player will win the game, output "Suzukaze becomes a grandmaster!"(without quotes). Otherwise, output "Suzukaze loses all his ratings!"(without quotes).

## Examples

|  | stdin | stdout |
| :--- | :--- | :--- |
| 8 | 6 |  |
| 1 | 2 |  |
| 2 | 3 |  |
| 4 | 5 |  |
| 5 | 6 |  |
| 6 | 7 |  |
| 7 | 8 |  |


|  | stdin | stdout |
| :--- | :--- | :---: |
| 2 | 1 |  |
| 1 | 2 | Suzukaze becomes a grandmaster! |

## Problem B. Bigram Language Model

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 5 seconds |
| Memory limit: | 256 MB |

In natural language processing, language models gives how likely a certain English sentence appear in a context (e.g. casual conversations, academic papers, or news websites) by assigning a probability distribution over all possible sentences. Bigram language model approaches this modeling problem by estimating the transition probabilities from previous word to next word. Formally,

$$
P\left(S=w_{1} w_{2} \ldots w_{m}\right)=P\left(w_{1}\right) P\left(w_{2} \mid w_{1}\right) \ldots P\left(w_{m} \mid w_{m-1}\right)
$$

We can estimate transition probabilities from word $s$ to $t$ from a corpus (a collection of sentences) collected from the context:

$$
P(t \mid s)=\frac{c(s, t)}{\sum_{t^{\prime} \in V} c\left(s, t^{\prime}\right)}
$$

where $V$ denotes the vocabulary (aka set of all words in the corpus), and $c(s, t)$ denotes the total number of times that word $t$ comes right after word $s$ in the same sentence in the corpus.

Suzukaze has collected a corpus and is trying to compute the probability of some sentences. He needs your help to get some transition probabilities. Can you help him?

## Input

The first line contains an integer $n(1 \leq n \leq 1000)$, the number of sentences in the corpus.
In the following $n$ lines, the $i$-th line starts with an integer $m_{i}\left(1 \leq m_{i} \leq 100\right)$, the number of words in the $i$-th sentence. It is then followed by $m_{i}$ space-separated words.
The next line contains an integer $q\left(1 \leq q \leq 10^{4}\right)$, the number of queries.
In the following $q$ lines, each line contains two space-separated words $s$ and $t$, querying for the estimated transition probability from word $s$ to $t$.
All words in the corpus and queries are no more than 10 characters long and contain lowercase letters only.

## Output

For each query, output a line containing the estimated transition probability for the queried word pair. Print the number as an irreducible fraction. (See example for details)
If you cannot estimate the transition probability from the corpus, print "Insufficient data"instead.

UIUC ICPC Spring Coding Contest 2019
University of Illinois at Urbana-Champaign, Saturday, April 13th, 2019

## Examples

| stdin |  |
| :--- | :--- |
| 5 | $1 / 1$ |
| 7 get busy living or get busy dying | $1 / 2$ |
| 4 stay hungry stay foolish | $1 / 1$ |
| 6 whatever you do do it well | Insufficient data |
| 6 everything you can imagine is real | $1 / 2$ |
| 5 the things you can find | $1 / 3$ |
| 8 | $2 / 3$ |
| get busy | $0 / 1$ |
| busy living |  |
| hungry stay |  |
| foolish stay |  |
| do do |  |
| you do |  |
| you can |  |
| can do |  |

## Problem C. Corns

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 3 seconds |
| Memory limit: | 256 MB |

pittoresque is a corn lover and he eats corns every day. One day he visited a new corn shop and decided to purchase some corns for his meal. pittoresque brought a $W$ dollar bill with him and he always spends as much money as he can to buy corns. To be specific, pittoresque wants to choose some corns such that the sum of their price is no larger than $W$, and is maximum among all possible choices of corns.

## Input

The first line contains two integers $n$ and $W\left(1 \leq n \leq 2 \times 10^{5}, 1 \leq W \leq 2 \times 10^{5}\right)$, the number of corns and the bill pittoresque brought.
In the following $n$ lines, the $i$-th line contains a single integer $p_{i}\left(1 \leq p_{i} \leq 2 \times 10^{5}\right)$, the price of corn $i$. It is guaranteed that $\sum_{i} p_{i} \leq 2 * 10^{5}$.

## Output

Output the maximum sum of price of corns that pittoresque can purchase.

## Examples

|  | stdin | stdout |
| :--- | :--- | :--- |
| 310 | 2 |  |
| 1 |  |  |
| 11 |  |  |


|  | stdin |
| :--- | :--- |
| 410 | 10 |
| 3 |  |
| 5 |  |
| 3 |  |
| 4 |  |

## Problem D. Dinner

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 3 seconds |
| Memory limit: | 256 MB |

A group of students gathered on a 2D plane for dinner. Before enjoying the feast, they decided to count how many groups of students are in a good position. A group of at least 3 students are in good position if and only if they form a convex polygon, that is, if a line is drawn between any two students, then the line should lie inside, or on the boundary of the polygon.
Please help them count the number of such group of students, such that they are in a good position. Since the output may be large, output the number module $10^{9}+7$.

## Input

The first line contains an integer $n(1 \leq n \leq 300)$, the length of the initial array. Each line in the next $n$ lines contains two numbers, $x_{i}, y_{i},\left|x_{i}\right|,\left|y_{i}\right| \leq 10^{6}$, the position of the $i^{t h}$ student on the plane. It is further guaranteed that no three students lie on a same line, and no two students have a same x coordinate, and no two students have a same y coordinate.

## Output

Output a single number, the number of groups are students that are in a good position, module $10^{9}+7$.

## Examples

|  | stdin |  |
| :--- | :--- | :--- |
| 3 |  | 1 |
| 1 | 1 | stdout |
| 12 |  |  |


|  | stdin |  | stdout |
| :--- | :--- | :--- | :--- |
| 5 |  | 13 |  |
| 0 | 0 |  |  |
| -1 | 1 | 4 |  |
| 2 | 7 |  |  |
| 1 | 3 |  |  |


|  | stdin |  |
| :--- | :--- | :--- |
| 4 |  | 4 |
| 0 | 0 |  |
| 4 | 1 |  |
| 1 | 4 |  |
| 2 | 2 |  |

## Problem E. Egma Game

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 2 seconds |
| Memory limit: | 256 MB |

As we all know, TiChuot97 is one of the greatest professional gamers of all time. And, similar to other great gamers, he loves games, especially nim games. Today, he just found out an online nim game Egma. As other nim games, Egma requires proficiency in computing mex values in order to master it. TiChuot97 understands that, just like millions of other games he mastered, Egma requires practicing. This is where his best friend, tourist, comes in to help.
tourist has prepared a drill for TiChuot97's practice. Initially, TiChuot97 is given an array of size $n$ of nonnegative integers $a_{1}, a_{2}, \ldots, a_{n}$. Then, tourist will give TiChuot97 $q$ queries each consists of two numbers $l, r(1 \leq l \leq r \leq n)$ asking for the mex of $\left\{a_{l}, a_{l+1}, \ldots, a_{r}\right\}$. Of course, TiChuot97 finished this drill easily. However, he thinks that this challenge can improve, not only his mex-computing skill, but also his programming skill. Do you also want to give this challenge a try?
Note: Mex value of a set of nonnegative integers is defined to be the minimum nonnegative integer that does not belong to the set.

## Input

The first line contains an integer $n\left(1 \leq n \leq 5 \times 10^{5}\right)$, the length of the initial array. The second line contains $n$ integers $a_{1}, a_{2}, \ldots, a_{n}\left(0 \leq a_{i} \leq 10^{9}\right)$. The third line contains an integers $q\left(1 \leq q \leq 5 \times 10^{5}\right)$, the number of queries. Each of the next $q$ lines contain a pair $l, r(1 \leq l \leq r \leq n)$ describing a query.

## Output

For each query, output on one line the answer to such query.

## Examples

|  |  |  |  | stdin |  | stdout |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 5 |  |  |  |  | 0 |  |
| 1 | 2 | 3 | 0 | 5 |  | 4 |
| 2 |  |  |  |  |  |  |
| 1 | 3 |  |  |  |  |  |
| 1 | 4 |  |  |  |  |  |

## Problem F. Fruit on the Tree

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 2 seconds |
| Memory limit: | 256 MB |

"Triangoes", a new type of fruit, are in triangular shapes and taste like mangoes. However, nobody in the world has ever seen "triangoes" since they always grow implicitly on the tree and hide in the triangles. Formally, a "triango" tree is an acyclic undirected connected graph with weighted edges and a "triango" is a set of three vertices on the "triango" tree such that the lengths of the three simple paths between each pair of these three vertices satisfy the triangle inequality; that is to say, they form a triangle.

After a long expedition, Suzukaze has eventually found a "triango" tree in his house. He needs your help to count the number of "triangoes" on the "triango" tree. Can you help him?

## Input

The first line contains an integer $n\left(1 \leq n \leq 10^{5}\right)$, the number of vertices on the "triango" tree. The vertices on the "triango" tree are labeled from 1 to $n$.
In the following $n-1$ lines, each of the lines contains 3 integers $u, v, w\left(1 \leq u, v \leq n, u \neq v, 1 \leq w \leq 10^{5}\right)$, which means that there is an undirected edge with weight $w$ connecting vertex $u$ and vertex $v$.
It's guaranteed that the input data is an acyclic undirected connected graph.

## Output

Output an integer - the number of "triangoes" on the "triango" tree.

## Examples

|  | stdin | stdout |  |
| :--- | :--- | :--- | :--- |
| 7 |  |  |  |
| 1 | 2 | 1 |  |
| 1 | 3 | 1 |  |
| 2 | 4 | 1 |  |
| 2 | 5 | 1 |  |
| 3 | 6 | 1 |  |
| 3 | 7 | 1 |  |

## Problem G. Greenberg Mass Comparison

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 1 second |
| Memory limit: | 256 MB |

Linguist Joseph Greenberg proposed the method of mass comparison for determining genetic relatedness between languages. In this method, $N$ languages are categorized into one or more families. Formally, given a set of $N$ different languages $\mathcal{L}=\left\{L_{1}, \ldots, L_{N}\right\}$, a relation analysis is a set of families $\mathcal{F}$, satisfying the following properties:

- $\mathcal{F}=\left\{F_{1}, \ldots, F_{k}\right\}$ for some $k$
- For $1 \leq i \leq k, F_{i} \subseteq \mathcal{L}$ and $F_{i} \neq \varnothing$
- For $1 \leq i, j \leq k, i \neq j, F_{i} \cap F_{j}=\varnothing$
- $\cup_{1 \leq i \leq k} F_{i}=\mathcal{L}$

Greenberg wants to know how many distinct relation analysis are there for $N$ languages. Two relation analyses $\mathcal{F}_{1}$ and $\mathcal{F}_{2}$ are distinct if $\mathcal{F}_{1} \neq \mathcal{F}_{2}$. Can you help him compute this number?

## Input

The first line of input contains a single integer $T(1 \leq T \leq 100)$, the number of test cases. In the following $T$ lines, each line contains a single integer $N(1 \leq N \leq 100)$.

## Output

For each test case, output a line containing the answer for the queried $N$, modulo $\left(10^{9}+7\right)$.

## Examples

|  | stdin | stdout |
| :--- | :--- | :--- |
| 4 | 1 |  |
| 1 |  | 2 |
| 2 | 5 |  |
| 3 | 840750853 |  |
| 40 |  |  |

## Problem H. Hamiltonian Farm

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 3 seconds |
| Memory limit: | 256 MB |

Last year, your team failed on helping the Codefalser Suzukaze AK the problemset. Therefore, Suzukaze decided to retire from competitive programming and became a farmer since he wants to own a farm as pittoresque does. Suzukaze is an orange-lover so he decided to plant only orange trees in his farm in spring. Winter is coming next week! Suzukaze is planning to walk inside his farm to harvest his favorite fruit. However, as a forgetful farmer, Suzukaze loses his memory about the configuration of his farm. Fortunately, as a careful programmer, Suzukaze stored the configuration of his farm in the computer as a function in case of he gets into this kind of desperate situation.
The farm can be modelled as a graph with $n$ vertices where vertices are orange trees, and the edges in the graph can be derived from the function $f$ :

$$
f(i, j)= \begin{cases}0 & i=j \\ \left((i p)^{j q} \bmod \left(10^{9}+7\right)\right) \bmod 2 & i<j \\ 1-f(j, i) & i>j\end{cases}
$$

where $i$ and $j$ are the indices of the vertices $(1 \leq i, j \leq n), p$ and $q$ are non-negative integers less than $10^{9}+7$. If $f(i, j)=1$, there is a directed edge from $i$ to $j$.
As a lazy farmer, Suzukaze wants to find a path that can visit each orange tree exactly once. Can you help him find this path in compensation for your failure last year?

## Input

The first line contains three integers $n, p$ and $q\left(1 \leq n \leq 10^{5}, 0 \leq p, q<10^{9}+7, p\right.$ and $q$ can't be 0 at the same time), the number of orange trees and the parameters of the function. You may assume that the orange trees have indices $1, \ldots, n$.

## Output

If the path exists, output the vertices on the path from the beginning vertex to the end vertex as the example shows. Any of the path that satisfies Suzukaze 's demand will be accepted. Otherwise, output -1 , which means that you fail on Suzukaze 's request again.

## Examples

|  | stdin |  | stdout |
| :--- | :--- | :--- | :--- |
|  | 1 | 1 | 1 |
|  |  |  |  |
|  |  | 3 |  |
|  |  | 5 |  |
|  |  | 4 |  |
|  |  | 2 |  |

## Explanation

The path $1 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$ satisfies Suzukaze 's demand in the example.

## Problem I. Innovative Alignment

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 2 seconds |
| Memory limit: | 256 MB |

Stringers can only read books if the $i$ 'th word of consecutive sentences start at the same position. If this condition is not met, they cannot read their books, and get rather upset. Can you help the Stringers by aligning all the given words correctly?

## Input

The first line contains one integer $n(1 \leq n \leq 10)$, representing the number of sentences you will be given to align.
The next $n$ lines that follow contain the sentences to align. Each sentence contains up to 10 words, and each word has up to 10 characters. The alphabet for this problem will only consist of uppercase and lowercase English letters.

## Output

Output the correct alignment of the input strings, such that the $i$ 'th word of each sentence starts at the same index. Note that when aligning words, there is always a space between the longest $i$ 'th word of any sentence and the first position of the alignment of the $i+1^{\prime}$ th words. Please take a look at the examples (specifically the second) below for clarification.

## Examples

|  | stdin |
| :--- | :--- |
| 2 | Hello World |
| Hello World | UoI IPL |
| UoI IPL |  |


| stdin | stdout |
| :--- | :--- |
| 3 | Align my life plz |
| Align my life plz | CTCI sucks |
| CTCI sucks |  |
| Welcome to check in to check in |  |

## Explanation

In the second example, the most important thing to note is the space between the second 's' in 'sucks' and the first alignment position for 'life' and 'check' (i.e. you can think about the index of the second 's' in 'sucks' is 12 and the index of the beginning of 'life' and 'check' is 14).

## Problem J. Juicy

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 5 seconds |
| Memory limit: | 256 MB |

Farmer pittoresque has a farm planted with two types of fruit, apples and bananas. Every fall, pittoresque needs to walk inside his farm to harvest these delicious fruits. However, as a banana-lover, pittoresque only cares about collecting bananas and doesn't care about how many apples he harvested.
The farm can be modelled as a graph where vertices are apple trees or banana trees, and there is an additional vertex indicating the entrance of the farm. To prepare for harvesting, pittoresque needs to build (bidirectional) roads throughout his farm between vertices. The roads must be built such that it is possible to reach every banana tree from the entrance. As a dedicated person, pittoresque gains some happiness during road building, despite spending some energy. Energy and happiness may be different for different roads. Nevertheless, pittoresque doesn't want to build roads that form a cycle, nor does he want to build roads that he cannot reach. Finally, pittoresque wants to maximize the ratio of sum of all happiness gained and sum of all energy consumed after he build the roads.

## Input

The first line contains two integers $a$ and $b(0 \leq a \leq 10,1 \leq b \leq 100)$, the number of apple trees and the number of banana trees. You may assume that the apple trees have index $1, \ldots, a$, the banana trees have index $a+1, \ldots, a+b$ and the entrance have index $a+b+1$.

Next line contains a single integer $m, b \leq m \leq 1000$, the number of roads that can be built.
Next $m$ lines contain information about the roads that can be built. Each line contains four integers $u, v, h, e, 1 \leq u, v \leq a+b+1, u \neq v, 0 \leq h \leq 10^{6}, 1 \leq e \leq 10^{6}$. This means that if a road connecting $u$ and $v$ is built, $e$ energy is consumed and $h$ happiness is gained.

It is guaranteed that it is possible to reach every banana tree from the entrance. Between two vertices, multiple roads may exist.

## Output

The maximum ratio between sum of all happiness gained and sum of all energy consumed, among all configuration of road building that satisfy the aforementioned constraints, can be expressed as $P / Q$, where $P$ and $Q$ are integers and they are co-prime. For your convenience, you just need to output $P \times Q$.

UIUC ICPC Spring Coding Contest 2019
University of Illinois at Urbana-Champaign, Saturday, April 13th, 2019

## Examples

|  |  |  | stdin |  | stdout |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 3 |  |  |  | 10 |
| 4 |  |  |  |  |  |
| 1 | 2 | 10 | 1 |  |  |
| 2 | 3 | 10 | 1 |  |  |
| 3 | 4 | 10 | 1 |  |  |
| 1 | 5 | 10 | 1 |  |  |


|  |  | stdin |  | stdout |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 3 |  |  | 2300046 |
| 5 |  |  |  |  |
| 1 | 2 | 100000 | 1 |  |
| 2 | 3 | 0 | 20 |  |
| 3 | 4 | 1 | 1 |  |
| 4 | 5 | 1 |  |  |
| 2 |  |  |  |  |
| 2 | 5 | 1 | 400 |  |

## Problem K. Koolhash

| Input file: | stdin |
| :--- | :--- |
| Output file: | stdout |
| Time limit: | 2 seconds |
| Memory limit: | 256 MB |

tourist has thought of a new hashing function to store administrator records, and he's enlisted you to help him build it! His hash function $\phi(n)$ will output a single integer, and needs the following pieces of information: $l, r$, and $N$, where $l$ represents the leftmost bit of $n, r$ represents the rightmost bit of $n$, and $N$ represents the number of 1-bits in $n$.

There aren't too many administrator records, so for now let's assume an unsigned 32-bit number system. Your job is to provide tourist with the three components of his hashing function given the number of records $k$, and the unique identifier of each record $n$. And yes, please forget about the absurdity of his hashing algorithm. Unfortunately, tourist has never taken a formal CS class.

## Input

The first line contains the number of records $k, 1 \leq k \leq 500$.
Each of the next $k$ lines contains an integer representing a record identifier $n, 0 \leq n<2^{31}$.
You can assume all inputs are given in decimal, and you need to convert them into 32-bits unsigned integers to get $l, r$ and $N$ for each $n$.

## Output

On each line, print three space-separated integers for every input record, denoting the leftmost bit $l$ of $n$, the rightmost bit $r$ of $n$, and number of 1-bits $N$ of $n$, respectively.

For further clarification, see the explanation provided for the first example below.

## Examples

|  | stdin | 001 |
| :--- | :--- | :--- |
| 1 |  |  |


|  | stdin |  |  | stdout |
| :--- | :--- | :--- | :--- | :--- |
| 3 | 0 | 1 | 4 |  |
| 45 | 0 | 0 | 2 |  |
| 68 | 0 | 1 | 4 |  |
| 23 |  |  |  |  |

## Explanation

For the first example, 8 is represented as $0 x 00000008$ (written in hexadecimal for simplicity). Thus, the left most bit is 0 , the right most bit is 0 , and the number of 1 -bits is 1 .

