

J — Joint Jog Jam

Problem

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Statistics at 4-hour mark: 274 submissions, 189 accepted, first after 00:10