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Statistics: 11 submissions, 3 accepted, 8 unknown

BAPC 2021



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 For calculating the next row, iterate over all rows that support a can placement and take the best.

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Number of can placements is F_{m+1} , the (m+1)th Fibonacci number. Time complexity: $\mathcal{O}(n \cdot F_{m+1}^2) = \mathcal{O}(n \cdot 3.3^m)$ when using bitmasks.

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