Problem J. Fun Region

Input file:	`standard input`
Output file:	`standard output`
Time limit:	2 seconds
Memory limit:	256 mebibytes

Dr. Ciel lives in a planar island with a polygonal coastline. She loves strolling on the island along spiral paths. Here, a path is called spiral if both of the following are satisfied.

- The path is a simple planar polyline with no self-intersections.

- At all of its vertices, the line segment directions turn clockwise.

Four paths are depicted below. Circle markers represent the departure points, and arrow heads represent the destinations of paths. Among the paths, only the leftmost is spiral.
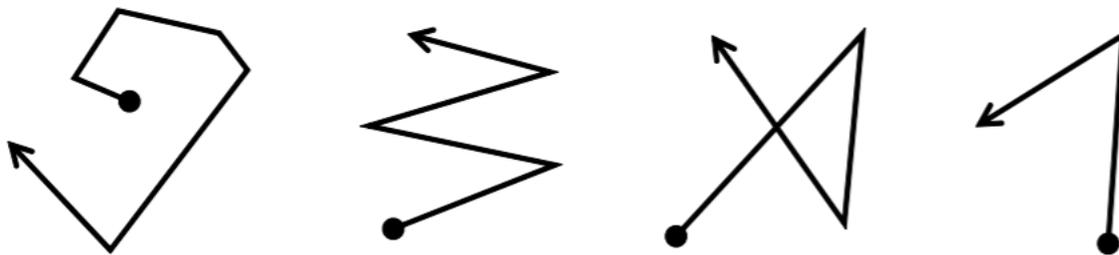
Dr. Ciel finds a point *fun* if, for all of the vertices of the islands coastline, there exists a spiral path that starts from the point, ends at the vertex, and does not cross the coastline. Here, the spiral path may touch or overlap the coastline.

In the following figure, the outer polygon represents a coastline. The point, labeled by star, is fun, while the point, labeled by cross. is not fun. Dotted polylines starting from star are valid spiral paths that end at coastline vertices.
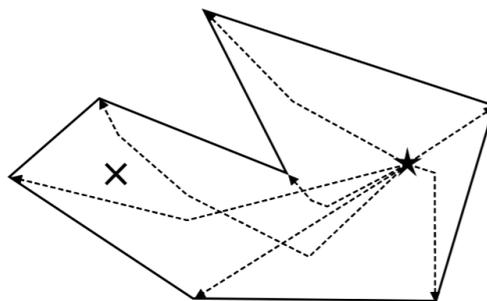
We can prove that the set of all the fun points forms a (possibly empty) connected region, which we call the fun region. Given the coastline, your task is to write a program that computes the area size of the fun region.

Input

First line of the input contains one integer n — the number of vertices of the polygon that represents the coastline ($3 \leq n \leq 2000$). Each of the following n lines has two integers x_i and y_i, which give the coordinates (x_i, y_i) of the i-th vertex of the polygon, in counterclockwise order. x_i and y_i are between 0 and 10^4, inclusive. Here, the x-axis of the coordinate system directs right and the y-axis directs up. The polygon is simple, that is, it does not intersect nor touch itself. Note that the polygon may be non-convex. It is guaranteed that the inner angle of each vertex is not exactly 180 degrees.

Output

Output the area of the fun region in one line. Absolute or relative errors less than 10^{-7} are permissible.

Examples

standard input	standard output
4 10 0 20 10 10 30 0 10	300.00
10 145 269 299 271 343 193 183 139 408 181 356 324 176 327 147 404 334 434 102 424	12658.3130191
6 144 401 297 322 114 282 372 178 197 271 368 305	0.0

Note

Figure below visualizes the three samples given below. The outer polygons correspond to the islands coastlines. The fun regions are shown as the gray areas.