

## G • Triangular N-Queens Problem

A “queen” piece on a triangular array of cells,  $N$  cells on a side, can attack any cell on a file parallel to one of the sides containing the queen’s cell. For example, in the array in Figure 1, a queen on the black cell, attacks all of the shaded cells. The Triangular N-Queens Problem of size  $N$ , is to find a maximal set of queen positions in a triangular array with  $N$  cells on a side so that no queen is attacking any other queen. For example, the black cells in Figure 2 give a maximal set of queen positions in a size 6 array. It turns out that a size  $N$  array always has  $\text{floor}((2*N + 1)/3)$  as the maximal number of non-attacking queen positions.

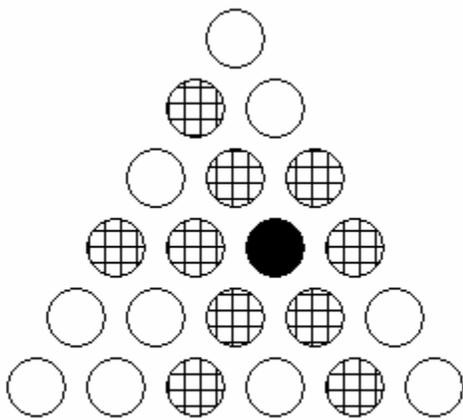


Figure 1

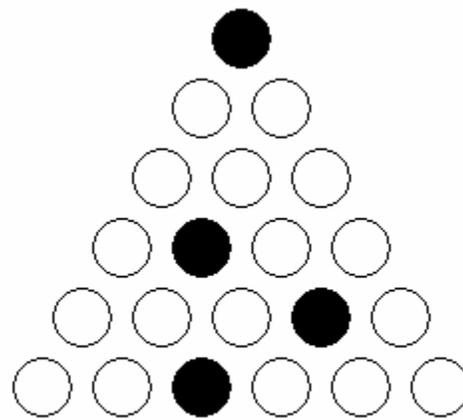


Figure 2

Write a program, which, given the size,  $N$ , of the triangular array, finds a maximal set of non-attacking queen positions on the array ( $\text{floor}((2*N + 1)/3)$  of them).

### Input

The input begins with a line containing an integer value specifying the number of datasets that follow,  $C$ , ( $1 \leq C \leq 1000$ ). Each dataset consists of a single line containing a single integer  $N$ , ( $1 \leq N \leq 1000$ ), which is the size of the triangular array.

### Output

The first output line for each problem gives the problem number starting at 1, a single space, the input size, a single space and the number of queen positions. Following the first line will be the queen positions, 8 positions per line except perhaps for the last line of positions. Each position has the format open bracket ('['), row number starting with 1, a comma, the position from the left within the row starting at 1 and a close bracket (']'). Positions within a line are separated by a single space. For example, the queen positions in Figure 2 are [1,1] [4,2] [5,4] [6,3]. The lines of position values are followed by a single blank line.



Sample Input	Sample Output
6	1 3 2
3	[1,1] [3,2]
6	
9	2 6 4
10	[3,1] [4,3] [5,5] [6,2]
14	
18	3 9 6
	[4,1] [5,3] [6,5] [7,7] [8,2] [9,4]
	4 10 7
	[4,1] [5,3] [6,5] [7,7] [8,2] [9,4] [10,6]
	5 14 9
	[6,1] [7,3] [8,5] [9,7] [10,9] [11,11] [12,2] [13,4]
	[14,6]
	6 18 12
	[7,1] [8,3] [9,5] [10,7] [11,9] [12,11] [13,13] [14,2]
	[15,4] [16,6] [17,8] [18,10]

## Notes

1. There may be many different correct answers to a particular problem, so your answers need not be the same as those in the **Sample Output** above.
2. Some solution methods for this problem may cause the time limit to be exceeded. Be sure to try the larger values before submitting your solution.