## 2020 ICPC Asia Tehran Regional Contest

## Problem M : Stabbing Number

A histogram is a simple rectilinear polygon $H$ (i.e. the interior angle at each vertex is either $90^{\circ}$ or $270^{\circ}$ ) that has a horizontal edge seeing every point $q$ inside (i.e. the interior or the boundary of) $H$. Here, we say that an edge sees a point $q \in H$ if there is a vertical segment $s$ connecting $e$ to $q$ that is lying inside $H$.

Let $H$ be a histogram with $n$ vertices, and consider a decomposition $R$ of $H$ into rectangles whose sides are vertical or horizontal. The vertices of the rectangles need not all be vertices of $H$ : it is allowed to introduce additional vertices, on the boundary of $H$ and/or in its interior. The stabbing number of a horizontal or vertical segment $s$ inside $H$ with respect to such a decomposition $R$ is the number of rectangles from $R$ whose interior (not just their boundaries) are intersected by $s$. The stabbing number of $R$ is the maximum stabbing number of any horizontal or vertical segment $s$ that lies inside $H$. The goal is to compute a decomposition $R$ with the minimum stabbing number.

## Input

The first line of the input contains two positive integers $m$ and $n(1 \leqslant m, n \leqslant 50)$ denoting the number of rows and the number of columns of the table illustrating the histogram, respectively. The next $m$ lines, each contains exactly $n$ characters. "*"s denote the boundary of the histogram. The rest is filled with dots ("."). Each edge of the histogram contains at least three "*"s. You can assume the given histogram has at least four and at most 16 edges, and edges do not overlap, intersect or touch each other; i.e. each " $\star$ " is adjacent to exactly two other "*" characters.

## Output

Print the stabbing number of the given histogram in one line.

## Example

| Standard Input | Standard Output |
| :---: | :---: |
| 1013 | 2 |
| * |  |
| . . . ${ }^{*}$. ** |  |
| $\ldots . . .{ }^{*} .{ }^{* * *}$. |  |
| ....**....*.. |  |
| .....***** |  |
| $\ldots{ }^{* * *} \ldots . .{ }^{*}$ |  |
| . . .*........* |  |
| ****.......** |  |
| * . . . . . . . . * |  |
| ************* |  |

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| Standard Input | Standard Output |
| :---: | :---: |
| 815 | 2 |
|  |  |
| ....***..*...*. |  |
|  |  |
| .*...........**. |  |
| **************. |  |

