## GCD-sum

| task: gcds | input file: stdin | output file: stdout |
| :--- | :--- | :--- |
| points: 100 | time limit: 2000 ms | memory limit: 1 GB |

## Task

A multi-set (i.e. a set with possible repetitions) of $n$ integers is given. We split the set into $k$ disjoint groups, for every group we compute the greatest common divisor of its elements, and sum all the subsets' GCDs.

For every $k=1,2, \ldots, n$, determine the maximal sum which can be obtained this way.

## Input

In the first line of input there is a single integer $n(1 \leq n \leq 500000)$ - the cardinality of the set. In the second line, there are $n$ positive integers, not exceeding $10^{12}$ - the given sequence.

## Output

Output $n$ line scontaining one integer each - the best sum of GCDs when partitioning into $1,2, \ldots, n$ subsets.

## Subtasks

| Subtask | Constraints | Points |
| :---: | :--- | :---: |
| 1 | $n \leq 7$ | 5 |
| 2 | $n \leq 15$ | 5 |
| 3 | $n \leq 100, a_{i} \leq 500$ | 8 |
| 4 | $n \leq 2000, a_{i} \leq 2000, a_{i}$ are distinct | 8 |
| 5 | $n \leq 2000$ | 14 |
| 6 | $a_{i}$ are distinct | 25 |
| 7 | no additional constraints | 35 |

## Samples

| input |  |  |  | output |
| :--- | :--- | :--- | :--- | :--- |
| 4 |  |  | 1   <br> 10 9 3 | 1 <br> 13 <br> 23 <br> 32 |

For $k=2$, the best partition is $(10,10)$ and $(9,3)$, giving the sum of $10+3=13$. For $k=3$, the best partition is $(10),(10)$ and $(9,3)$ with the sum of 23 .


