## Problem J. Graph and Cycles

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
2 seconds
256 megabytes

There is an undirected weighted complete graph of $n$ vertices where $n$ is odd.
Let's define a cycle-array of size $k$ as an array of edges $\left[e_{1}, e_{2}, \ldots, e_{k}\right]$ that has the following properties:

- $k$ is greater than 1 .
- For any $i$ from 1 to $k$, an edge $e_{i}$ has exactly one common vertex with edge $e_{i-1}$ and exactly one common vertex with edge $e_{i+1}$ and these vertices are distinct (consider $e_{0}=e_{k}, e_{k+1}=e_{1}$ ).

It is obvious that edges in a cycle-array form a cycle.
Let's define $f\left(e_{1}, e_{2}\right)$ as a function that takes edges $e_{1}$ and $e_{2}$ as parameters and returns the maximum between the weights of $e_{1}$ and $e_{2}$.
Let's say that we have a cycle-array $C=\left[e_{1}, e_{2}, \ldots, e_{k}\right]$. Let's define the price of a cycle-array as the sum of $f\left(e_{i}, e_{i+1}\right)$ for all $i$ from 1 to $k$ (consider $e_{k+1}=e_{1}$ ).
Let's define a cycle-split of a graph as a set of non-intersecting cycle-arrays, such that the union of them contains all of the edges of the graph. Let's define the price of a cycle-split as the sum of prices of the arrays that belong to it.

There might be many possible cycle-splits of a graph. Given a graph, your task is to find the cycle-split with the minimum price and print the price of it.

## Input

The first line contains one integer $n(3 \leq n \leq 999, n$ is odd $)$ - the number of nodes in the graph.
Each of the following $\frac{n \cdot(n-1)}{2}$ lines contain three space-separated integers $u, v$ and $w$ $\left(1 \leq u, v \leq n, u \neq v, 1 \leq w \leq 10^{9}\right)$, meaning that there is an edge between the nodes $u$ and $v$ that has weight $w$.

## Output

Print one integer - the minimum possible price of a cycle-split of the graph.

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## Examples

|  |  | standard input |  |
| :--- | :--- | :--- | :--- |
| 3 |  | 3 |  |
| 1 | 2 | 1 |  |
| 2 | 3 | 1 |  |
| 3 | 1 | 1 |  |
| 5 |  |  |  |
| 4 | 5 | 4 |  |
| 1 | 3 | 4 |  |
| 1 | 2 | 4 |  |
| 3 | 2 | 3 |  |
| 3 | 5 | 2 |  |
| 1 | 4 | 3 |  |
| 4 | 2 | 2 |  |
| 1 | 5 | 4 |  |
| 5 | 2 | 4 |  |
| 3 | 4 | 2 |  |

## Note

Let's enumerate each edge in the same way as they appear in the input. I will use $e_{i}$ to represent the edge that appears $i$-th in the input.

The only possible cycle-split in the first sample is $S=\left\{\left[e_{1}, e_{2}, e_{3}\right]\right\} . f\left(e_{1}, e_{2}\right)+f\left(e_{2}, e_{3}\right)+f\left(e_{3}, e_{1}\right)=1+1+1=3$.
The optimal cycle-split in the second sample is $S=\left\{\left[e_{3}, e_{8}, e_{9}\right],\left[e_{2}, e_{4}, e_{7}, e_{10}, e_{5}, e_{1}, e_{6}\right]\right\}$. The price of [ $e_{3}, e_{8}, e_{9}$ ] is equal to 12 , the price of $\left[e_{2}, e_{4}, e_{7}, e_{10}, e_{5}, e_{1}, e_{6}\right]$ is equal to 23 , thus the price of the split is equal to 35 .

