

Problem I

Critical Structures

Time limit: 3 seconds

Memory limit: 1024 megabytes

Problem Description

Intelligence Cloud Privacy Company (ICPC) is a world famous cloud service company that aims at developing secure and powerful cloud computing environments for users. Engineers in the ICPC construct a data center with n computing nodes, denoted by $1, 2, \dots, n$, and m communication links. We can model this data center as an undirected graph $G = (V, E)$, in which n vertices represent n computing nodes and an edge between Node i to Node j if there is a communication link between them; we also call i and j are two end-nodes of this link. In addition, for two arbitrary nodes i and j in G , there is at most one communication link between i and j , and there is no communication link between the same node.

A *linear array structure* in a data center G is a sequence of nodes $\langle v_0, v_1, \dots, v_{k-1} \rangle$, where $k \geq 2$, such that any two consecutive v_{i-1} and v_i for $1 \leq i \leq k-1$ have a communication link, and v_i for $0 \leq i \leq k-1$ are all distinct. A *ring structure* is a sequence of nodes $\langle v_0, v_1, \dots, v_{k-1} \rangle$, where $k \geq 4$, such that any two consecutive v_{i-1} and v_i for $1 \leq i \leq k-1$ have a communication link, $v_0 = v_{k-1}$ and v_i for $0 \leq i \leq k-2$ are all distinct. A data center G is *connected* if there is a linear array between any two nodes; otherwise, it is *disconnected*. Using some elegant resource allocation algorithm, a research team of the ICPC needs to find the following critical structures for enhancing the privacy and security:

1. Critical node: a node in G whose removal disconnects G .
2. Critical link: a communication link in G whose removal disconnects G .
3. Critical component: a maximal set of communication links in G such that any two communication links in the set lie on a common ring.
4. Largest critical component: a critical component with the maximum number of communication links.

Given a connected data center G , your task is to write a computer program for computing the number of critical nodes, the number of critical links, and

$$\begin{aligned} \mu^* &= \frac{\text{the number of critical components}}{\text{the number of communication links in a largest critical component}} \\ &= \frac{p}{q}, \end{aligned}$$

where $\frac{p}{q}$ is an irreducible form of μ^* .

Input Format

The first line of the input file contains an integer L ($L \leq 10$) that indicates the number of test cases as follows. For each test case, the first line contains two integers (separated by a space) representing n and m . Then it is immediately followed by m lines, in which each line contains two integers that represent two end-nodes of a communication link; moreover, any two consecutive integers are separated by a space.

Output Format

The output contains one line for each test case. Each line contains four positive integers representing the number of critical nodes, the number of critical links, p , and q , where $\frac{p}{q}$ is an irreducible form of μ^* . Note that any two consecutive integers are separated by a space.

Technical Specification

- $3 \leq n \leq 1000$ for each test case.
- $n - 1 \leq m \leq \frac{n(n-1)}{2}$.
- The sum of m in all L tests is smaller than 10^6 .

Sample Input 1

```
1
6 6
1 2
2 3
3 4
4 5
5 6
6 1
```

Sample Output 1

```
0 0 1 6
```

Sample Input 2

```
1
6 7
1 2
2 3
3 1
4 5
5 6
6 4
1 4
```

Sample Output 2

2 1 1 1
