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## Problem K Tiling Polyomino Time Limit: 1.5 Seconds

A polyomino is a plane geometric figure formed by joining one or more unit squares edge to edge. The figure below shows two examples of polyominos. Each of the squares contained in a polyomino is called a cell, and two cells sharing an edge are called neighbors of each other. Note that the number of neighbors of a cell can be 0, 1, 2, 3 and 4. A polyomino *P* is called connected if every pair of cells (a, b) in *P* has a path connecting neighboring cells from *a* to *b*, and *P* is called simply connected if *P* is connected and does not contain any "hole". In the figure below, the left one is simply connected but the right one is not. We will deal with a simply connected polyomino *P* such that every cell contained in *P* has two or more neighbors.



A tiling of a polyomino P is a tessellation (covering using geometric shapes with no overlaps and no gaps) of P by translated copies of D1, D2, T1, and T2, where D1 (resp. D2) is a polyomino formed by joining two unit squares horizontally (resp. vertically), and T1 (resp. T2) is a polyomino formed by joining three unit squares horizontally (resp. vertically). The figure below shows D1, D2, T1, and T2. According to the shape of P, a tiling of P may or may not exist.



To represent a polyomino P, we assume that P is contained in an  $n \times n$  unit square grid. We label each unit square s in the grid as 1 if s is a cell of P, or 0 otherwise. Then, the unit square grid containing P can be represented by an  $n \times n$  matrix of 0's and 1's. A tiling of P can also be represented by an  $n \times n$  matrix of integers as follows. If a cell of P is covered by a copy of D1 or D2, then we label the cell as 2 or 3, respectively. If a cell of P is covered by T1 or T2, then we label the cell as 4 or 5, respectively. The figure below shows an example of tiling and its representation.

| 0 | 1 | 1 | 1 | 1 | 1 |   | 0 | 5 | 3 | 5 | 3 | 3 |
|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 0 | 1 | 1 | 1 | 1 | 1 |   | 0 | 5 | 3 | 5 | 3 | 3 |
| 0 | 1 | 1 | 1 | 0 | 0 |   | 0 | 5 | 3 | 5 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | _ | 0 | 0 | 3 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 1 | 1 | [ | 2 | 2 | 2 | 2 | 2 | 2 |
|   | - | - |   |   | _ |   |   |   |   |   |   |   |

ICPC 2020 Asia Regional – Seoul Problem K: Tiling Polyomino

Given a simply connected polyomino P such that every cell contained in P has two or more neighbors represented by an  $n \times n$  matrix of 0's and 1's, write a program that outputs a tiling of P, if it exists.

## Input

Your program is to read from standard input. The input starts with a line containing an integer  $2 \le n \le 1,000$ , where *n* is the number of rows and columns of the unit square grid containing a polyomino *P*. Each of the following *n* lines contains *n* many 0's and 1's, and 1 denotes that the square is a cell of *P*. The polyomino *P* is simply connected and every cell contained in *P* has two or more neighbors.

## Output

Your program is to write to standard output. If there is a tiling of P, print the tiling of P using n lines. Each of the n lines contains n integers from 0 to 5. A 0 represents that the square is not a cell of P. A 2 represents that the square is a cell of P, and is covered by D1. Similarly, a 3, 4, or 5 represents that the square is a cell of P, and is covered by D2, T1, or T2, respectively. If there is no possible tiling of P, then print -1.

The following shows sample input and output for two test cases.

| Sample Input 1 | Output for the Sample Input 1 |
|----------------|-------------------------------|
| 3              | 022                           |
| 011            | 322                           |
| 111            | 322                           |
| 111            |                               |

| Sample Input 2 | Output for the Sample Input 2 |
|----------------|-------------------------------|
| 6              | 053533                        |
| 011111         | 053533                        |
| 011111         | 053500                        |
| 011100         | 003000                        |
| 001000         | 22222                         |
| 111111         | 44444                         |
| 111111         |                               |