

## Problem H

### Hamiltonian Hypercube

Hypercube graphs are fascinatingly regular, hence you have devoted a lot of time studying the mathematics related to them. The vertices of a hypercube graph of dimension  $n$  are all binary strings of length  $n$ , and two vertices are connected if they differ in a single position. There are many interesting relationships between hypercube graphs and error-correcting code.

One such relationship concerns the  $n$ -bit Gray Code, which is an ordering of the binary strings of length  $n$ , defined recursively as follows. The sequence of words in the  $n$ -bit code first consists of the words of the  $(n - 1)$ -bit code, each prepended by a 0, followed by the same words in reverse order, each prepended by a 1. The 1-bit Gray Code just consists of a 0 and a 1. For example the 3-bit Gray Code is the following sequence:

000, 001, 011, 010, 110, 111, 101, 100

Now, the  $n$ -bit Gray Code forms a Hamiltonian path in the  $n$ -dimensional hypercube, i.e., a path that visits every vertex exactly once (see Figure H.1).

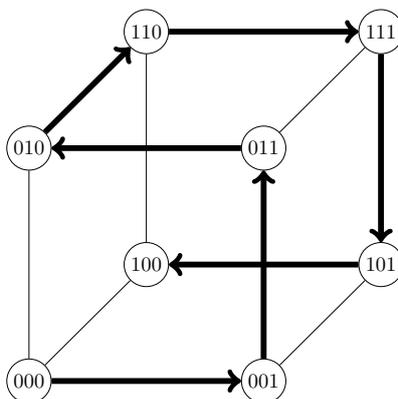


Figure H.1: The 3-dimensional hypercube and the Hamiltonian path corresponding to the 3-bit Gray Code.

You wonder how many vertices there are between the vertices  $0^n$  ( $n$  zeros) and  $1^n$  ( $n$  ones) on that path. Obviously it will be somewhere between  $2^{n-1} - 1$  and  $2^n - 2$ , since in general  $0^n$  is the first vertex, and  $1^n$  is somewhere in the second half of the path. After finding an elegant answer to this question you ask yourself whether you can generalise the answer by writing a program that can determine the number of vertices between two arbitrary vertices of the hypercube, in the path corresponding to the Gray Code.

### Input

The input consists of a single line, containing:

- one integer  $n$  ( $1 \leq n \leq 60$ ), the dimension of the hypercube
- two binary strings  $a$  and  $b$ , both of length  $n$ , where  $a$  appears before  $b$  in the  $n$ -bit Gray Code.

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## Output

Output the number of code words between  $a$  and  $b$  in the  $n$ -bit Gray Code.

### Sample Input 1

3 001 111

### Sample Output 1

3

### Sample Input 2

3 110 100

### Sample Output 2

2