

## Problem K Kiwi Trees

You are about to plant a pair of fine kiwi trees inside your big property. You are worried that tree branches would grow beyond the boundaries of your property, making your neighbours complain. You must also avoid planting the two trees too close to each other so that the branches of the trees grow into each other, because that could lead to a loss of fruit.

The seller of the trees guaranteed that no branch or leaf will be farther than 4 meters from the trunk of its tree, thus we will model the trees as circles of radius 4 meters. The trunks are perfectly vertical.

Local government regulations forbid certain shapes of properties. In particular, in order for government employees to be able to draw and handle maps of the area, each property must satisfy the following properties:

1. The boundary is a simple polygon, i.e. the sides are non-intersecting and form a closed path.
2. Each side length of the property is at least 30 meters long.
3. The angle between any two consecutive sides of the property must be at least 18 degrees (10% of a straight angle), and at most 144 degrees (80% of a straight angle, or if you will, the angle of a regular decagon).

Non-convex properties are allowed as long as the angles of consecutive sides follow rule 3 above, so the inner angle at a vertex can also be between  $360 - 144 = 216$  and  $360 - 18 = 342$  degrees. See Figure K.1 for an example.

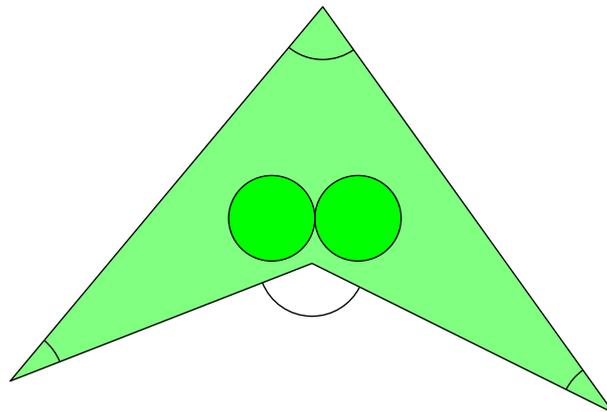


Figure K.1: Illustration of Sample Input 1 and the solution given in Sample Output 1. All the marked angles are at least 18 and at most 144 degrees.

Your property follows these rules. Can you plant two trees inside the property such that their branches and leaves do not grow beyond its boundary, and that the branches and leaves of each tree do not grow into the other tree?



Photo by Nathaniel Hayag, cc by-nd

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## Input

The input consists of:

- One line containing an integer  $n$ , where  $3 \leq n \leq 2000$  is the number of vertices of the polygon describing your property.
- $n$  lines describing one vertex each. Each such line contains two integers  $x$  and  $y$ , where  $0 \leq x, y \leq 10^7$ . These two numbers denote the  $x$ - and  $y$ -coordinates of a vertex in *millimeters*, in a clockwise order as they appear in the polygon.

Also, each polygon side is at least 30 meters (30 000 millimeters) long and the angle of two segments at a vertex is at least 18 degrees and at most 144 degrees. The polygon is non-intersecting and closed, i.e. the last vertex is connected to the first vertex.

## Output

If it is possible to plant two trees without their branches growing beyond the boundary of your property or into each other, output two lines, each containing two real numbers  $x$  and  $y$  giving the coordinates in millimeters of two points where the trees can be planted.

Otherwise, print “impossible”.

You may assume that increasing or decreasing the radius by 1 mm will not change whether or not it is possible to plant the trees. Your answer will be accepted if the tree locations are at least 3999 mm away from the boundary and at least  $2 \cdot 3999$  mm away from each other.

### Sample Input 1

```
4
0 3000
29000 38000
56000 0
28000 14000
```

### Sample Output 1

```
32266.13633130 18219.22050526
24266.13633130 18219.22050526
```

### Sample Input 2

```
3
50000 50000
69500 73000
99000 80000
```

### Sample Output 2

```
impossible
```