

2020 Canadian Computing Olympiad
Day 1, Problem 3
Mountains and Valleys

Time Limit: 7 seconds

Problem Description

You are planning a long hiking trip through some interesting, but well-known terrain. There are N interesting sites you would like to visit and M trails connecting pairs of sites. Each trail has a difficulty level indicated as a positive integer.

The trail system is a bit special, however. There are exactly $N - 1$ trails with difficulty level 1 (these are completely flat trails), and the rest of the trails all have a difficulty level of at least $\left\lceil \frac{N}{3} \right\rceil$ (these are very mountainous trails). (The ceiling of x , denoted as $\lceil x \rceil$, is the smallest integer greater than or equal to x .)

Additionally, it is possible to travel between any two sites using only the trails with difficulty level 1.

You would like to visit every site, starting your walk from any site of your choice and finishing at some other site, such that you visit each site at least once and the total sum of difficulty levels is minimum among all walks. Note that walking a trail k times with difficulty level d contributes a value of $k \cdot d$ to the sum of difficulty levels.

Input Specification

The first line of input contains two space-separated integers N ($4 \leq N \leq 500\,000$) and M ($N - 1 \leq M \leq 2\,000\,000$).

The next M lines contain three space-separated integers x_i, y_i , and w_i describing the trail between sites x_i and y_i with difficulty level w_i ($1 \leq i \leq M$; $0 \leq x_i, y_i \leq N - 1$; $x_i \neq y_i$). Note that there is at most one trail between every pair of sites, and that $w_i = 1$ or $\left\lceil \frac{N}{3} \right\rceil \leq w_i \leq N$.

For 1 of the 25 marks available, $N \leq 6$ and $M \leq 10$.

For an additional 2 of the 25 marks available, $N \leq 20$ and $M \leq 40$.

For an additional 2 of the 25 marks available, $N \leq 5\,000$, $M \leq 10\,000$, and either $w_i = 1$ or $\left\lceil \frac{N}{2} \right\rceil \leq w_i \leq N$.

For an additional 6 of the 25 marks available, $N \leq 100$ and $M \leq 200$.

For an additional 2 of the 25 marks available, $N \leq 500$ and $M \leq 1\,000$.

For an additional 3 of the 25 marks available, $N \leq 5\,000$ and $M \leq 10\,000$.

For an additional 5 of the 25 marks available, $N \leq 80\,000$ and $M \leq 160\,000$.

Output Specification

Output one integer, which is the minimum sum of difficulty levels taken for all trails walked to visit each site at least once.

Sample Input

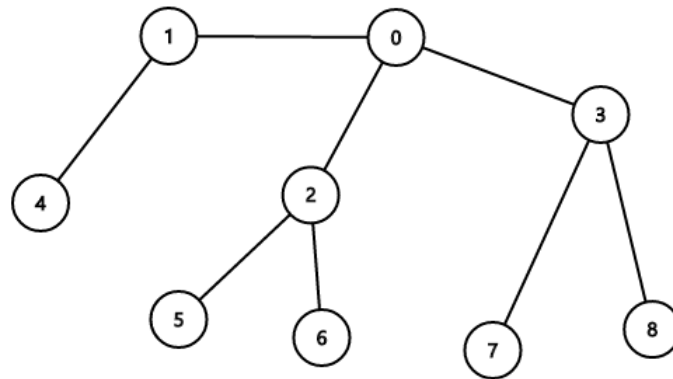
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9 10
0 1 1
0 2 1
0 3 1
1 4 1
2 5 1
2 6 1
3 7 1
3 8 1
2 4 5
6 7 3
```

Output for Sample Input

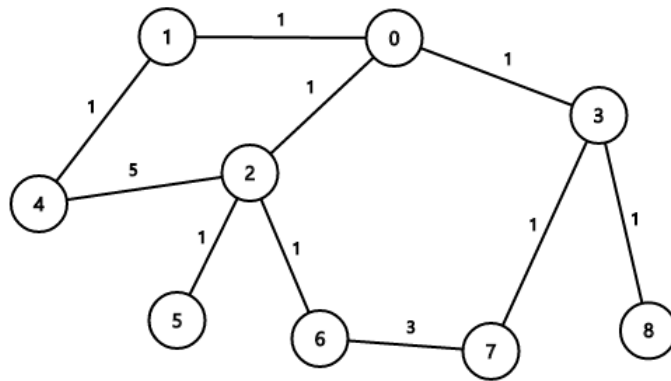
11

Explanation of Output for Sample Input

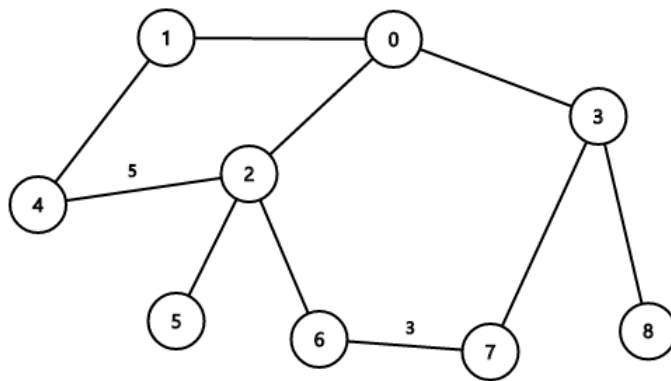
This is the set of flat trails:



This is the entire set of trails with all the difficulty levels.



This is the entire set of trails, with trails with difficulty level 1 being omitted.



An optimal walk for this set of trails is $4 \rightarrow 1 \rightarrow 0 \rightarrow 2 \rightarrow 5 \rightarrow 2 \rightarrow 6 \rightarrow 7 \rightarrow 3 \rightarrow 8$ with a total cost of $1 + 1 + 1 + 1 + 1 + 1 + 3 + 1 + 1 = 11$. There is no way to make a walk that visits all the sites at least once with a lower total difficulty level cost.