

## F. Graph Theory

Bobo has an **undirected** graph  $G$  with  $n$  vertices labeled by  $1, \dots, n$  and  $n$  edges. For each  $1 \leq i \leq n$ , there is an edge between the vertex  $i$  and the vertex  $(i \bmod n) + 1$ . He also has a list of  $m$  pairs  $(a_1, b_1), \dots, (a_m, b_m)$ .

Now, Bobo is going to choose an  $i$  and remove the edge between the vertex  $i$  and the vertex  $(i \bmod n) + 1$ . Let  $\delta_i(u, v)$  be the number of edges on the shortest path between the  $u$ -th and the  $v$ -th vertex **after the removal**. Choose an  $i$  to minimize the maximum among  $\delta_i(a_1, b_1), \dots, \delta_i(a_m, b_m)$ .

Formally, find the value of

$$\min_{1 \leq i \leq n} \left\{ \max_{1 \leq j \leq m} \delta_i(a_j, b_j) \right\}.$$

### Input

The input consists of several test cases terminated by end-of-file. For each test case,

The first line contains two integers  $n$  and  $m$ .

For the following  $m$  lines, the  $i$ -th line contains two integers  $a_i$  and  $b_i$ .

- $2 \leq n \leq 2 \times 10^5$
- $1 \leq m \leq 2 \times 10^5$
- $1 \leq a_i, b_i \leq n$  for each  $1 \leq i \leq m$
- In each input, the sum of  $n$  does not exceed  $2 \times 10^5$ . The sum of  $m$  does not exceed  $2 \times 10^5$ .

### Output

For each test case, output an integer which denotes the minimum value.

### Sample Input

```
3 2
1 2
2 3
3 2
1 1
2 2
3 3
1 2
2 3
3 1
```

### Sample Output

```
1
0
2
```

### Note

For the first case,

$i$	$\delta_i(1, 2)$	$\delta_i(2, 3)$
1	2	1
2	1	2
3	1	1

Choosing  $i = 3$  yields the minimum value 1.