

## Problem B Circle Bounce Time Limit: 1 Second(s)

You are standing by the wall in a large, perfectly circular arena and you throw a tennis ball hard against some other part of the arena. After a given number of bounces, where does the tennis ball next strike the wall?

Map the arena as a unit circle centered at the origin, with you standing at the point (-1,0). You throw the ball with a direction given by a slope in the coordinate plane of a rational fraction a/b. Each bounce is perfect, losing no energy and bouncing from the wall with the same angle of reflection as the angle of incidence to a tangent to the wall at the point of impact.



After n bounces, the ball strikes the circle again at some point p which has rational coordinates that can be expressed as (r/s, t/u). Output the fraction r/s modulo the prime M = 1,000,000,007.

It can be shown that the x coordinate can be expressed as an irreducible fraction r/s, where r and s are integers and  $s \not\equiv 0 \pmod{M}$ . Output the integer equal to  $r \cdot s^{-1} \pmod{M}$ . In other words, output an integer k such that  $0 \le k < M$  and  $k \cdot s \equiv r \pmod{M}$ .

For example, if we throw the ball with slope 1/2 and it bounces once, it first strikes the wall at coordinates (3/5, 4/5). After bouncing, it next strikes the wall at coordinates (7/25, -24/25). The modular inverse of 25 with respect to the prime M is 280,000,002, and the final result is thus  $7 \cdot 280,000,002 \pmod{M} = 960,000,007$ .

## Input

The single line of input will contain three integers a, b  $(1 \le a, b \le 10^9, \text{gcd}(a, b) = 1)$  and n  $(1 \le n \le 10^{12})$ , where a/b is the slope of your throw, and n is the number of bounces. Note that a and b are relatively prime.



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## Output

Output a single integer value as described above.

• Note that Sample 2 corresponds to the example in the problem description.

Sample Input 1	Sample Output 1
1 1 3	100000006

Sample Input 2	Sample Output 2
1 2 1	96000007

Sample Input 3	Sample Output 3
11 63 44	22

Sample Input 4	Sample Output 4
163 713 980	0