

## Problem I. Red Black Tree

Input file: *standard input*  
Output file: *standard output*  
Time limit: 2 seconds  
Memory limit: 512 mebibytes

You are given a rooted tree with  $n$  nodes. The nodes are numbered  $1..n$ . The root is node 1, and  $m$  of the nodes are colored red, the rest are black.

You would like to choose a subset of nodes such that there is no node in your subset which is an ancestor of any other node in your subset. For example, if A is the parent of B and B is the parent of C, then you could have at most one of A, B or C in your subset. In addition, you would like exactly  $k$  of your chosen nodes to be red.

If exactly  $m$  of the nodes are red, then for all  $k = 0..m$ , figure out how many ways you can choose subsets with  $k$  red nodes, and no node is an ancestor of any other node.

### Input

Each input will consist of a single test case. Note that your program may be run multiple times on different inputs. Each test case will begin with a line with two integers  $n$  ( $1 \leq n \leq 2 \times 10^5$ ) and  $m$  ( $0 \leq m \leq \min(10^3, n)$ ), where  $n$  is the number of nodes in the tree, and  $m$  is the number of nodes which are red. The nodes are numbered  $1..n$ .

Each of the next  $n - 1$  lines will contain a single integer  $p$  ( $1 \leq p \leq n$ ), which is the number of the parent of this node. The nodes are listed in order, starting with node 2, then node 3, and so on. Node 1 is skipped, since it is the root. It is guaranteed that the nodes form a single tree, with a single root at node 1 and no cycles.

Each of the next  $m$  lines will contain single integer  $r$  ( $1 \leq r \leq n$ ). These are the numbers of the red nodes. No value of  $r$  will be repeated.

### Output

Output  $m + 1$  lines, corresponding to the number of subsets satisfying the given criteria with a number of red nodes equal to  $k = 0..m$ , in that order. Output this number modulo  $10^9 + 7$ .

## Examples

standard input	standard output
4 1 1 1 1 3	5 4
4 4 1 1 1 1 1 2 3 4	1 4 3 1 0
14 4 1 2 1 2 3 4 5 5 13 8 10 4 4 8 3 12 13	100 169 90 16 0