

# Problem I: Insertion Order

A friend of yours is currently taking a class on algorithms and data structures. Just last week he learned about binary search trees and the importance of using self-balancing trees in order to keep the tree height low and guarantee fast access to every node.

Recall that a binary search tree is a binary tree with each node storing a key, and the property that the key of each node is greater than all keys in the left subtree of that node and less than all keys in the right subtree. A new key is inserted into the tree by adding a new leaf node with that key in the only position such that the property is maintained, as seen in the figure below.

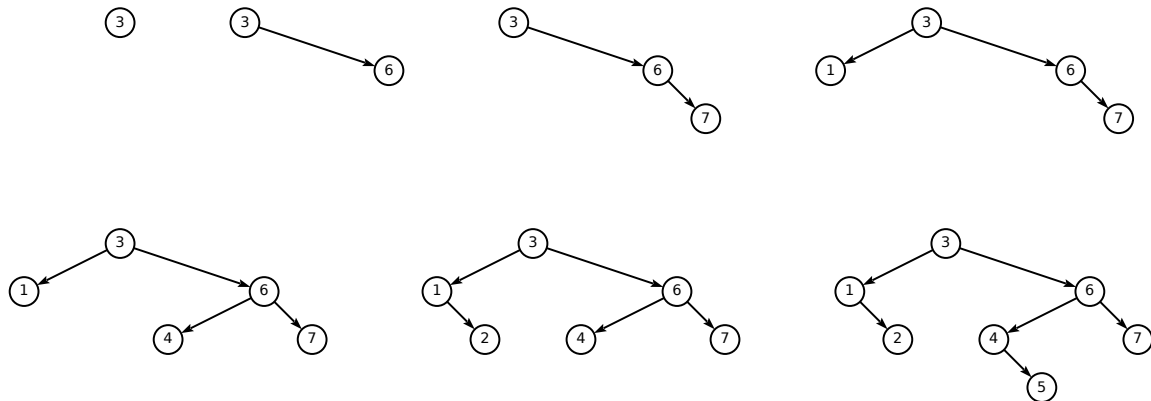


Figure I.1: Illustration of the first sample case.

To illustrate to him just how bad things can get without self-balancing, you want to show him that it is possible to build trees of nearly any height by carefully choosing an insertion order.

You are given two integers  $n$  and  $k$  and want to construct a binary search tree with  $n$  nodes of height  $k$  (the height of a tree is the maximal number of nodes on a path from the root to a leaf). To do so, you need to find a permutation of the integers from 1 to  $n$  such that, when they are inserted into an empty binary search tree in that order (without self-balancing), the resulting tree has height  $k$ .

## Input

The input consists of two integers  $n$  and  $k$  ( $1 \leq k \leq n \leq 2 \cdot 10^5$ ), where  $n$  is the number of nodes in the tree and  $k$  is the exact height the tree should have.

## Output

If there is no solution, output `impossible`. Otherwise, output one line with  $n$  integers, the requested permutation. If there is more than one solution, any one of them will be accepted.

### Sample Input 1

7 4

### Sample Output 1

3 6 7 1 4 2 5

### Sample Input 2

8 3

### Sample Output 2

impossible