

# Problem I: Index Case

The epidemiologist W. Andy wants to find the index case of an ongoing crisis. To do this, he modelled the city of the outbreak and its  $n$  residents with a *cellular automaton*. The city is represented by  $n$  cells numbered from 1 to  $n$  and each cell has two neighbouring cells, one to its left and one to its right. The left neighbour of cell  $i$  is cell  $i - 1$  and the right neighbour is cell  $i + 1$ . Additionally, the left neighbour of cell 1 is cell  $n$  and the right neighbour of cell  $n$  is cell 1. Thus, the city and the corresponding automaton form a simple cycle.

Each cell contains an integer between 1 and  $m$  which represents how likely it is that this person is infected. Since the virus can only be transmitted by personal contact, the value in the  $i$ th cell on day  $d$  only depends on the values of its neighbours and itself on the previous day. If we denote this value by  $s_d[i]$ , then the outbreak can be simulated by a function  $f$  using the formula:

$$s_d[i] = f(s_{d-1}[i-1], s_{d-1}[i], s_{d-1}[i+1]).$$

Note that as the city is cyclic both  $i + 1$  and  $i - 1$  are calculated modulo  $n$ .

Andy wants to find the index case, so he first has to find  $s_0$ , the state of the city on day zero. This poses a problem, however, as it is not known on which day the crisis started. Right now, Andy believes that he accomplished the task and found the state  $s_0$ , but you are not convinced. Therefore, you want to check if there may be a state previous to the initial state proposed by Andy, i.e. whether there exists any state  $s_{-1}$  that gets transformed into  $s_0$  by applying  $f$ .

## Input

The input consists of:

- One line with two integers  $n$  and  $m$  ( $3 \leq n \leq 200, 2 \leq m \leq 10$ ), the number of cells and the number of states.
- $m^3$  lines describing the values  $f(x, y, z)$  ( $1 \leq f(x, y, z) \leq m$  for each  $1 \leq x, y, z \leq m$ ) of the function  $f$  modelling the automaton. The values are given in lexicographic order of the arguments: The first value is  $f(1, 1, 1)$ , the next is  $f(1, 1, 2)$ , and so on until  $f(1, 1, m)$ , followed by  $f(1, 2, 1)$  and so forth. The last value is  $f(m, m, m)$ .
- One line with  $n$  integers  $s_0[1], \dots, s_0[n]$  ( $1 \leq s_0[i] \leq m$  for each  $i$ ), the initial state that has been proposed by Andy.

## Output

Output `yes` if there exists at least one possible previous state and `no` otherwise.

### Sample Input 1

```
4 2
1
2
1
2
2
2
1
2
1
1 2 1 2
```

### Sample Output 1

```
yes
```

**Sample Input 2**

```
6 2
1
2
1
2
2
1
2
1
1 2 1 2 1 2
```

**Sample Output 2**

```
no
```

**Sample Input 3**

```
10 2
1
2
1
1
2
2
2
2
2
1 2 2 2 1 2 1 2 1 2
```

**Sample Output 3**

```
yes
```