



2022 ICPC Taiwan Online Programming Contest

# Problem E Etched Emerald Orbs

Time limit: 3 seconds Memory limit: 1024 megabytes

# **Problem Description**

An archaeologist team found a tomb of the ancient tribe and discovered  $2^{125}$  emerald orbs inside the tomb. The ancient tribe etched a numbers on each emerald orb. The archeologists spent two decades realizing that the ancient tribe etched each emerald orb with a unique number. Moreover, the numbers are from 1 to  $2^{125}$  in the ancient language.

Eddy, the only mathematician in the archaeologist team, recently figured out the relation between the number k and the emerald orb numbered k. The weight of the emerald orb numbered k is exactly  $\frac{1}{k}$  grams. Since the number on each emerald orb is distinct from the number on any other emerald orb, there are no two emerald orbs having the same weight.

Eddy proposes a hypothesis: the ancient tribe used these emerald orbs to represent weight less than 1 gram. It is trivial that the emerald orb numbered k can represent  $\frac{1}{k}$  gram. Then, Eddy tries to represent  $\frac{2}{k}$  grams for  $3 \le k \le 4 \times 10^{18}$  with two emerald orbs. He successfully finds that the emerald orbs numbered 2 and 6 can represent  $\frac{2}{3} = \frac{1}{2} + \frac{1}{6}$  grams. Similarly, the emerald orbs numbered 3 and 15 can represent  $\frac{2}{5} = \frac{1}{3} + \frac{1}{15}$  grams.

Can you write a program to help Eddy to check whether two emerald orbs can represent  $\frac{2}{k}$  grams for a given integer k? If there are multiple combinations of two emerald orbs representing  $\frac{2}{k}$  grams, output the combination minimizing the sum of the numbers etched on them. If there is no such combination, output -1.

## **Input Format**

The input contains only one positive integer k.

# **Output Format**

If there is no solution, output -1. Otherwise, output two distinct integers x and y separated by a blank where  $\frac{2}{k} = \frac{1}{x} + \frac{1}{y}$  and  $1 \le x < y \le 2^{125}$ . If there are multiple solutions, output the solution minimizing x + y.

## **Technical Specification**

•  $3 \le k \le 4 \times 10^{18}$ .

## Sample Input 1

#### 5

#### Sample Output 1

3 15





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## Sample Input 2

7

# Sample Output 2

4 28