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## Problem H Longest Substring Time Limit: 5.0 Seconds

For a string S of length  $n \ge 1$  and a positive integer k  $(1 \le k \le n)$ , a non-empty substring of S is called a ksubstring if the substring appears exactly k times. Such k occurrences are not necessarily disjoint, i.e., are possibly overlapping. For example, if S = "ababa", the k-substrings of S for every k = 1, ..., 5 are as follows:

- There are four 1-substrings in S, "abab", "ababa", "bab", and "baba" because these substrings appear exactly once in S. Note that "aba" is not a 1-substring because it appears twice.
- There are four 2-substrings in *S*, "ab", "aba", "b", and "ba". The substring "ab" appears exactly twice without overlapping. Two occurrences of the substring "aba" are overlapped at a common character "a", but it does not appear three times or more.
- There is only one 3-substring in *S*, "a".
- Neither 4-substrings nor 5-substrings exist in *S*.

For a k-substring T of S, let d(T) be the maximum number of the disjoint occurrences of T in S. For example, a 2-substring T = "ab" can be selected twice without overlapping, that is, the maximum number of the disjoint occurrences is two, so d(T) = 2. For a 2-substring T = "aba", it cannot be selected twice without overlapping, so d(T) = 1. For a 3-substring T = "a", it can be selected three times without overlapping, which is the maximum, so d(T) = 3.

Let f(k) be the length of the longest one among all k-substring T with the largest d(T) for  $1 \le k \le n$ . For example, f(k) for S = "ababa" and k = 1, ..., 5 is as follows:

- For k = 1, all 1-substrings T can be selected only once without overlapping, so d(T) = 1. Thus, the longest one among all 1-substrings with d(T) = 1 is "ababa", so f(1) = 5.
- For k = 2, d(T) = 1 for T = "aba", but d(T) = 2 for the other 2-substrings T = "ab", "b", "ba". Among 2-substrings with d(T) = 2, "ab" and "ba" are the longest ones, so f(2) = 2.
- For k = 3, f(3) = 1 because there is only one 3-substring "a".
- For k = 4, 5, there are no k-substrings, so f(4) = 0 and f(5) = 0.

Given a string S of length n, write a program to output n values of f(k) from k = 1 to k = n. For the above example, the output should be 5 2 1 0 0.

## Input

Your program is to read from standard input. The input starts with a line containing the string *S* consisting of n ( $1 \le n \le 50,000$ ) lowercase alphabets.

## Output

Your program is to write to standard output. Print exactly one line. The line should contain exactly n non-negative integers, separated by a space, that represent f(k) from k = 1 to k = n in order, that is,  $f(1) f(2) \dots f(n)$ . Note that f(k) should be zero if there is no k-substring for some k.

The following shows sample input and output for two test cases.

Sample Input 1	Output for the Sample Input 1
ababa	5 2 1 0 0
Sample Input 2	Output for the Sample Input 2
aaaaaaa	8 7 6 5 4 3 2 1