



Naan

JOI Curry Shop is famous for serving very long naans. They have L kinds of flavors, numbered from 1 through L , to flavor naans. “JOI Special Naan” is the most popular menu in the shop. The length of the naan is L cm. We define “the position x ” as the position on the naan which is x cm distant from the left end of the naan. The segment between position $j - 1$ and position j is flavored by flavor j ($1 \leq j \leq L$).

N people came to JOI Curry Shop. Their preferences are different from each other. Specifically, when the i -th ($1 \leq i \leq N$) person eats naan with flavor j ($1 \leq j \leq L$), they will get happiness $V_{i,j}$ per 1 cm.

They ordered only one JOI Special Naan. They will share the naan in the following manner:

1. Choose $N - 1$ rational numbers X_1, \dots, X_{N-1} which satisfy $0 < X_1 < X_2 < \dots < X_{N-1} < L$.
2. Choose N integers P_1, \dots, P_N which form a permutation of $1, \dots, N$.
3. For each k ($1 \leq k \leq N - 1$), cut the naan at the position X_k . Thus, the naan will be separated into N pieces.
4. For each k ($1 \leq k \leq N$), give the piece between the position X_{k-1} and position X_k to the P_k -th person. We consider X_0 as 0 and X_N as L .

We want to distribute the naan fairly. We say a distribution is **fair** if each person gets happiness of more than or equal to $\frac{1}{N}$ of the amount of happiness they will get by eating the whole JOI Special Naan.

Write a program which, given the information of preferences of N people, determines if it is possible to distribute the naan in a fair way, and if it is possible, finds such a fair way.

Input

Read the following data from the standard input. All the values in the input are integers.

```
N L
V1,1 V1,2 ⋯ V1,L
⋮
VN,1 VN,2 ⋯ VN,L
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Output

Write to the standard output. If it is impossible to distribute naan in a fair way, write -1 in a line. If it is possible, output $N - 1$ rational numbers X_1, \dots, X_{N-1} and N integers P_1, \dots, P_N which represent a fair distribution, in the following format.

$$\begin{array}{l} A_1 B_1 \\ A_2 B_2 \\ \vdots \\ A_{N-1} B_{N-1} \\ P_1 P_2 \cdots P_N \end{array}$$

A_k and B_k are a pair of integers which satisfies $X_k = \frac{A_k}{B_k}$ ($1 \leq k \leq N - 1$). These integers have to follow the “Constraints of Output” section.

Constraints of Input

- $2 \leq N \leq 2\,000$.
- $1 \leq L \leq 2\,000$.
- $1 \leq V_{i,j} \leq 100\,000$ ($1 \leq i \leq N$, $1 \leq j \leq L$).

Constraints of Output

If it is possible to distribute the naan in a fair way, the output must satisfy the following constraints:

- $1 \leq B_k \leq 1\,000\,000\,000$ ($1 \leq k \leq N - 1$).
- $0 < \frac{A_1}{B_1} < \frac{A_2}{B_2} < \dots < \frac{A_{N-1}}{B_{N-1}} < L$.
- P_1, \dots, P_N is a permutation of $1, \dots, N$.
- In the distribution, the amount of happiness which i -th person will get is more than or equal to $\frac{V_{i,1} + V_{i,2} + \dots + V_{i,L}}{N}$ ($1 \leq i \leq N$).

A_k and B_k are **not** necessary to be coprime ($1 \leq k \leq N - 1$).

Under the constraints of the input, it can be proved that if a fair distribution exists, there is a correct output which satisfies $1 \leq B_k \leq 1\,000\,000\,000$ ($1 \leq k \leq N - 1$).



Subtasks

1. (5 points) $N = 2$.
2. (24 points) $N \leq 6, V_{i,j} \leq 10$ ($1 \leq i \leq N, 1 \leq j \leq L$).
3. (71 points) No additional constraints.

Sample Input and Output

Sample Input 1	Sample Output 1
2 5	14 5
2 7 1 8 2	2 1
3 1 4 1 5	

In this sample, the first person will get happiness of $2 + 7 + 1 + 8 + 2 = 20$ when she eats the whole naan and the second person will get happiness of $3 + 1 + 4 + 1 + 5 = 14$ when she eats the whole naan. Thus, if the first person gets happiness of more than or equal to $\frac{20}{2} = 10$ and the second person gets happiness of more than or equal to $\frac{14}{2} = 7$, the distribution is fair.

If you cut the naan at the position $\frac{14}{5}$, the first person will get happiness of $1 \times \frac{1}{5} + 8 + 2 = \frac{51}{5}$ and the second person will get happiness of $3 + 1 + 4 \times \frac{4}{5} = \frac{36}{5}$. Hence, this is a fair distribution.

Sample Input 2	Sample Output 2
7 1	1 7
1	2 7
2	3 7
3	4 7
4	5 7
5	6 7
6	3 1 4 2 7 6 5
7	

In this sample, the naan has only one flavor. If you equally divide the naan into 7 pieces, the distribution will be fair, regardless of P_1, \dots, P_N .



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Contest Day 1 – Naan

Sample Input 3	Sample Output 3
5 3	15 28
2 3 1	35 28
1 1 1	50 28
2 2 1	70 28
1 2 2	3 1 5 2 4
1 2 1	

Note that A_k and B_k are not necessary to be coprime ($1 \leq k \leq N - 1$).