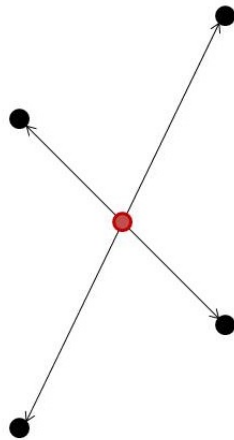


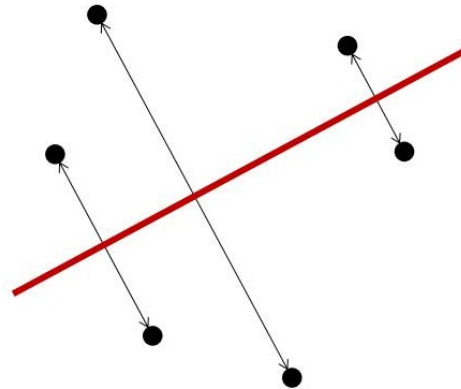
## Problem G

### Symmetry

You are totally bored with nothing to do. You notice a pattern of spots on the wall in front of you and begin to dwell on them. There is no obvious pattern of symmetry. With time this becomes very grating, and you contemplate adding more spots to satisfy your quest for balance. For this exercise you are to resolve this situation with a computer program.



Symmetry around a Point



Symmetry around a Line

Given an array of spots with coordinates in the range from  $-20,000$  to  $20,000$ , determine the fewest additional spots needed to generate a pattern with some symmetry. The symmetry can be around a point or across a line. If the symmetry is around a point, the point does not need to be a spot in the data, or even a point with integral coordinates. If the symmetry is across a line, the line may be at any angle. The coordinates of the additional spots may or may not be within the  $-20,000$  to  $20,000$  limits.

### Input

Each input will consist of a single test case. Note that your program may be run multiple times on different inputs. The first line of input will consist of a single integer  $n$  ( $1 \leq n \leq 1,000$ ) indicating the number of spots. Each of the next  $n$  lines will hold two space-separated integers  $x$  and  $y$  ( $-20,000 \leq x, y \leq 20,000$ ), which are the coordinates of a spot. The locations of all spots are guaranteed to be unique.



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## Output

Output a single integer, indicating the smallest number of spots which need to be added so that all of the spots are symmetric about some point, or about some line.

### Sample Input 1

```
4
0 0
1000 0
0 1000
1000 1000
```

### Sample Output 1

```
0
```

### Sample Input 2

```
11
0 0
70 100
24 200
30 300
480 400
0 100
0 200
0 400
100 0
300 0
400 0
```

### Sample Output 2

```
6
```