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## Problem I Tourists

In Tree City, there are $n$ tourist attractions uniquely labeled 1 to $n$. The attractions are connected by a set of $n-1$ bidirectional roads in such a way that a tourist can get from any attraction to any other using some path of roads.

You are a member of the Tree City planning committee. After much research into tourism, your committee has discovered a very interesting fact about tourists: they LOVE number theory! A tourist who visits an attraction with label $x$ will then visit another attraction with label $y$ if $y>x$ and $y$ is a multiple of $x$. Moreover, if the two attractions are not directly connected by a road the tourist will necessarily visit all of the attractions on the path connecting $x$ and $y$, even if they aren't multiples of $x$. The number of attractions visited includes $x$ and $y$ themselves. Call this the length of a path.

Consider this city map:


Here are all the paths that tourists might take, with the lengths for each:

To take advantage of this phenomenon of tourist behavior, the committee would like to determine the number of attractions on paths from an attraction $x$ to an attraction $y$ such that $y>x$ and $y$ is a multiple of $x$. You are to compute the sum of the lengths of all such paths. For the example above, this is: $4+3+2+2+3+4+3+3+2+5+6+2+3+3+3+4+3=55$.

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## Input

Each input will consist of a single test case. Note that your program may be run multiple times on different inputs. The first line of input will consist of an integer $n(2 \leq n \leq 200,000)$ indicating the number of attractions. Each of the following $n-1$ lines will consist of a pair of space-separated integers $i$ and $j(1 \leq i<j \leq n)$, denoting that attraction $i$ and attraction $j$ are directly connected by a road. It is guaranteed that the set of attractions is connected.

## Output

Output a single integer, which is the sum of the lengths of all paths between two attractions $x$ and $y$ such that $y>x$ and $y$ is a multiple of $x$.

| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 10 | 55 |
| 3 | 4 |
| 3 | 7 |
| 1 | 4 |
| 4 | 6 |
| 1 | 10 |
| 8 | 10 |
| 2 | 8 |
| 1 | 5 |
| 4 | 9 |

