

## Problem A. Graph Partitioning

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            **3 seconds**  
Memory limit:         **1024 megabytes**

Little Cyan Fish and Xiao Qing Yu are two good friends. Each of them has a rooted tree with  $n$  vertices. Each vertex is labeled from 1 to  $n$ . Recall that a tree is an undirected graph in which any two vertices are connected by exactly one path, or equivalently, a connected acyclic undirected graph. Let's denote  $par_T(x)$  as the parent vertex of  $x$  in the tree  $T$ .

The tree owned by Little Cyan Fish is called  $T_1$ . It has the following properties:

- $T_1(V_1, E_1)$  is a tree rooted at vertex 1.
- $\forall 2 \leq x \leq n$ , the index of the parent of  $x$  should be less than  $x$ .
  - Formally,  $par_{T_1}(x) < x$  for all  $2 \leq x \leq n$ .

The tree owned by Xiao Qing Yu is called  $T_2$ . It has the following properties:

- $T_2(V_2, E_2)$  is a tree rooted at vertex  $n$ .
- $\forall 1 \leq x < n$ , the index of the parent of  $x$  should be greater than  $x$ .
  - Formally,  $par_{T_2}(x) > x$  for all  $1 \leq x < n$ .

Since they are good friends, they want to merge their own trees into a larger graph. Suppose  $G = (V, E)$  is the new graph merged by their trees:

- $V$  is the same as  $V_1$  and  $V_2$ . In other words, the new graph also contains  $n$  vertices, and each vertex is labeled from 1 to  $n$ .
- $E$  is the union of  $E_1$  and  $E_2$ . If some edge appears in  $E_1$  and  $E_2$  simultaneously, it will appear in  $E$  twice.

Now you are given all the edges in  $G$ . Your task is to calculate how many different pairs of trees  $(T_1, T_2)$  could generate such a graph  $G$ . Two trees are considered different if and only if there exists an edge  $e$  that appears in one of the trees but not in the other one. Note that edges in  $G$  may appear more than once, and multiple edges are treated as different edges.

Since the answer can be quite large, you only need to output it modulo 998 244 353.

### Input

The first line of the input contains a single integer  $n$  ( $1 \leq n \leq 5 \times 10^5$ ).

The next  $2n - 2$  lines of the input describe the edges in  $E$ . The  $i$ -th line contains two integers  $u_i$  and  $v_i$ , indicating an edge  $(u_i, v_i) \in E$ . Note that if some edge appears in  $E_1$  and  $E_2$  simultaneously, it will appear in  $E$  twice.

Note that there might be multiple edges or self-loops in the graph. And it is possible that there's no valid pair of  $(T_1, T_2)$ .

### Output

Print a single line contains a single integer, indicating the answer modulo 998 244 353.

## Examples

standard input	standard output
2 1 2 1 2	2
1	1
3 1 2 2 3 1 3 2 2	0
6 3 4 1 3 3 5 1 6 6 5 4 2 5 4 1 2 4 1 5 3	2

## Note

In the first test case, note that multiple edges might exist. Since the two edges are different, so there are two possible pairs of  $(T_1, T_2)$ .

In the second test case, it is possible that the graph is empty. In this case, making both  $G_1$  and  $G_2$  empty is a possible choice.

In the third test case, note that there might be self-loops.