## Garden

JOI Kingdom is a mysterious kingdom which has a boundless expanse of territory. JOI-kun, the king of JOI Kingdom, is planning to cut a part of the territory and make his garden.

The territory of JOI Kingdom is considered as a sufficiently large 2-dimensional grid. The grid is paved with square cells from the top to the bottom and from the left to the right. There is a cell, which is the origin of the coordinates. Let $(x, y)$ denote the cell one arrives at when one moves from the origin to the right direction for the distance of $x$ cells and to the upward direction for the distance of $y$ cells. Here, the left direction for the distance of $a$ cells means the right direction for the distance of $-a$ cells. Similarly, the downward direction for the distance of $a$ cells means the upward direction for the distance of $-a$ cells.

Some artworks are placed on the territory. The artworks are classified into two types, Type A and Type B, according to the way to be placed in the territory.

- There are $N$ kinds of artworks of type A. An artwork of $i$-th kind $(1 \leq i \leq N)$ is placed on every cell of the form $\left(P_{i}+k D, Q_{i}+l D\right)$, where $k, l$ are integers.
- There are $M$ kinds of artworks of type B. An artwork of $j$-th kind $(1 \leq j \leq M)$ is placed on every cell of the form $\left(R_{j}+k D, y\right)$, where $k, y$ are integers, or of the form $\left(x, S_{j}+l D\right)$, where $l, x$ are integers.

Note that a cell may contain several artworks of different kinds.
JOI-kun is planning to choose a rectangular region on the grid to make a garden. In other words, he will choose 4 integers $a, b, c, d$. Then the cells of the form $(x, y)$, where $x, y$ are integers satisfying $a \leq x \leq b, c \leq y \leq$ $d$, will constitute JOI-kun's garden. Since JOI-kun likes to see artworks of many kinds, for any of the $N+M$ kinds of artworks, JOI-kun's garden should contain at least one artwork of that kind. On the other hand, the citizens of JOI Kingdom will be angry if JOI-kun plans to make a too large garden. Therefore, JOI-kun wants to minimize the number of cells in the garden so that the above condition is satisfied.

Write a program which, given information of artworks, calculates the minimum number of cells in JOI-kun's garden.

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## Input

Read the following data from the standard input.

$$
\begin{aligned}
& N M D \\
& P_{1} Q_{1} \\
& P_{2} Q_{2} \\
& \vdots \\
& P_{N} Q_{N} \\
& R_{1} S_{1} \\
& R_{2} S_{2} \\
& \vdots \\
& R_{M} S_{M}
\end{aligned}
$$

## Output

Write one line to the standard output. The output should contain the minimum number of cells in JOI-kun's garden.

## Constraints

- $N \geq 1$.
- $M \geq 1$.
- $N+M \leq 500000$.
- $1 \leq D \leq 5000$.
- $0 \leq P_{i}<D(1 \leq i \leq N)$.
- $0 \leq Q_{i}<D(1 \leq i \leq N)$.
- $0 \leq R_{j}<D(1 \leq j \leq M)$.
- $0 \leq S_{j}<D(1 \leq j \leq M)$.
- Given values are all integers.


## Subtasks

1. (15 point) $M \leq 8$.
2. (6 points) $D \leq 10, \quad N+M \leq 5000$.
3. (8 points) $D \leq 50, \quad N+M \leq 5000$.
4. (16 points) $D \leq 100, \quad N+M \leq 5000$.
5. (30 points) $N+M \leq 5000$.
6. (25 points) No additional constraints.

## Sample Input and Output

| Sample Input 1 | Sample Output 1 |
| :--- | :--- |
| 2 | 1 |
| 1 | 4 |
| 2 | 2 |
| 0 | 0 |

The following figure describes the cells $(x, y)$, where $x, y$ are integers satisfying $0 \leq x<10,0 \leq y<10$, in the territory of JOI Kingdom.


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In this figure, circles and diamond shapes are artworks of type $A$ and $B$, respectively. An integer in a circle or a diamond shape describes the kind of the artwork. If JOI-kun chooses $a=1, b=2, c=2, d=5$, JOI-kun's garden is a black rectangular region. In this case, JOI-kun's garden has at least one artwork of any of the 3 kinds of artworks. The number of cells in the garden is 8 . Since there is no garden which satisfies the condition and which has smaller number of cells, output 8 .

This sample input satisfies the constraints of all the subtasks.

| Sample Input 2 | Sample Output 2 |
| :--- | :--- |
| $3 \quad 4 \quad 100$ | 2840 |
| 2026 |  |
| 81 | 56 |
| 20 | 3 |
| 58 | 71 |
| 74 | 82 |
| 95 | 61 |
| 95 | 61 |$\quad$.

This sample input satisfies the constraints of Subtasks $1,4,5,6$.

| Sample Input 3 | Sample Output 3 |
| :--- | :--- |
| 575000 | 10543092 |
| 1046365 |  |
| 4122 1166 |  |
| 40092896 |  |
| 18154065 |  |
| 4372 1651 |  |
| 2382 123 |  |
| 1475836 |  |
| 3313 | 4005 |
| 2579 | 568 |
| 4300 | 4867 |
| 1050 | 3214 |
| 3589 | 4653 |

This sample input satisfies the constraints of Subtasks 1, 5, 6 .

