## Problem J. Jiry Matchings

| Input file: | standard input |
| :--- | :--- |
| Output file: | standard output |
| Time limit: | 6 seconds |
| Memory limit: | 512 mebibytes |

Ruyi Ji has a tree where the vertices are numbered by integers from 1 to $n$ and each edge has a weight. For each $k \leq(n-1)$, he asked you to find the largest total weight of a matching with $k$ edges if it exists.

## Input

The first line of input contains one integer $n$ : the number of vertices in the tree ( $2 \leq n \leq 200000$ ).
Each of the next $n-1$ lines contains three integers $u_{i}, v_{i}, w_{i}$, describing an edge from $u_{i}$ to $v_{i}$ with weight $w_{i}$ in the tree $\left(1 \leq u_{i}, v_{i} \leq n, u_{i} \neq v_{i},-10^{9} \leq w_{i} \leq 10^{9}\right)$.
It is guaranteed that the given graph is a tree.

## Output

Output $n-1$ integers: the largest weights of the matchings with $1,2, \ldots, n-1$ edges. If there is no such matching for the current $k$, print "?" instead.

## Examples

| standard input | standard output |
| :---: | :---: |
| $\begin{array}{lll} \hline 5 & & \\ 1 & 2 & 3 \\ 2 & 3 & 5 \\ 2 & 4 & 4 \\ 3 & 5 & 2 \end{array}$ | 56 ? ? |
| $\begin{array}{llll} \hline 10 & \\ 2 & 8 & -5 \\ 5 & 10 & 5 \\ 3 & 4 & -5 \\ 1 & 6 & 5 \\ 3 & 9 & 5 \\ 1 & 7 & -3 \\ 4 & 8 & -5 \\ 10 & 8 & -5 \\ 1 & 8 & -3 \end{array}$ | $5101510 \text { ? ? ? ? ? }$ |
| $\begin{array}{lll} \hline 2 & & \\ 1 & 2 & 35 \end{array}$ | 35 |

## Note

In the first sample, with $k=1$ you should take edge $(2,3)$ with weight 5 . And with $k=2$ you should take two edges, $(2,4)$ and $(3,5)$, with total weight 6 . There are no matchings with a greater number of edges.

