

# Cliques

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            5 seconds  
Memory limit:         512 megabytes

Given is a tree  $\mathcal{T}$  with  $n$  vertices numbered with consecutive natural numbers from 1 to  $n$ . Using it, we will create an undirected, initially empty graph  $\mathcal{G}$ . There are two types of operations to be performed:

- $+ v w$  ( $1 \leq v \leq w \leq n$ ) – a vertex is added to the graph  $\mathcal{G}$ , which is labeled with a pair of numbers  $(v, w)$ .
- $- v w$  ( $1 \leq v \leq w \leq n$ ) – one vertex labeled with the pair of numbers  $(v, w)$  is removed from the graph  $\mathcal{G}$ .

The pairs of numbers written in the vertices of graph  $\mathcal{G}$  correspond to paths from the given tree  $\mathcal{T}$  – these two numbers indicate the indices of the two ends of such a path, and they can be equal if the path consists of a single vertex.

At any given time, two vertices of the graph  $\mathcal{G}$  are connected by an edge if the paths from  $\mathcal{T}$  corresponding to them have at least one vertex in common. After adding a new vertex to the graph  $\mathcal{G}$ , edges are attached to it according to this rule, and when a vertex is removed, all the edges incident to it are also removed.

Your task is, after each operation, to output the number of non-empty subsets of vertices of the graph  $\mathcal{G}$  that form cliques. A clique is a subgraph in which every pair of vertices is connected by an edge. Since this number can be very large, it's sufficient to output its remainder when divided by  $10^9 + 7$ .

## Input

The first line of standard input contains one integer  $n$  ( $2 \leq n \leq 200\,000$ ), indicating the number of vertices of the tree  $\mathcal{T}$ .

Each of the next  $n - 1$  lines contains two integers. The numbers in the  $i$ -th of these lines are  $a_i$  and  $b_i$  ( $1 \leq a_i, b_i \leq n$ ), indicating the existence in the tree  $\mathcal{T}$  of an edge connecting vertices numbered  $a_i$  and  $b_i$ . It is guaranteed that the given edges describe a valid tree.

The next line contains one integer  $q$  ( $1 \leq q \leq 50\,000$ ), indicating the number of modifications to the graph  $\mathcal{G}$ .

Each of the next  $q$  lines is of one of the two possible types:

- $+ v w$  ( $1 \leq v \leq w \leq n$ ) – a vertex is added to the graph  $\mathcal{G}$ , corresponding to the path between vertices  $v$  and  $w$  of the tree  $\mathcal{T}$ .
- $- v w$  ( $1 \leq v \leq w \leq n$ ) – one vertex corresponding to the path between vertices  $v$  and  $w$  of the tree  $\mathcal{T}$  is removed from the graph  $\mathcal{G}$ .

**Multiple vertices in the graph  $\mathcal{G}$  can have the same pair of numbers written in them.** It's guaranteed that when instructed to remove a vertex with a certain pair of numbers, at least one such vertex exists in the graph  $\mathcal{G}$ . When instructed to remove, only one vertex with the corresponding path should be removed, even if more of them currently exist.

## Output

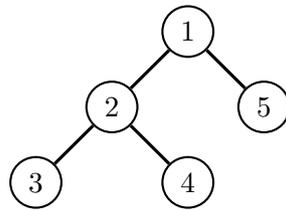
The output should contain  $q$  lines – the  $i$ -th of them should contain one integer, the number of non-empty subsets of vertices of the graph  $\mathcal{G}$  that form cliques after the  $i$ -th modification. This number should be given as a remainder when divided by  $10^9 + 7$ .

## Example

standard input	standard output
5	1
1 2	3
5 1	7
2 3	3
4 2	7
6	9
+ 4 5	
+ 2 2	
+ 1 3	
- 2 2	
+ 2 3	
+ 4 4	

## Note

The tree  $\mathcal{T}$  from the sample test looks as follows:

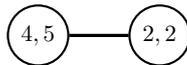


The following figures show the graph  $\mathcal{G}$  after consecutive modifications.

The graph  $\mathcal{G}$  after the first modification:

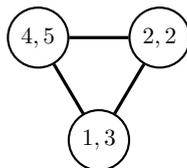


The graph  $\mathcal{G}$  after the second modification:

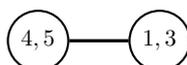


Both vertices in  $\mathcal{G}$  are connected by an edge because the common vertex in  $\mathcal{T}$  for both paths is vertex number 2.

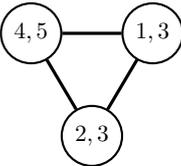
The graph  $\mathcal{G}$  after the third modification:



The graph  $\mathcal{G}$  after the fourth modification:



The graph  $\mathcal{G}$  after the fifth modification:



The graph  $\mathcal{G}$  after the last modification:

