

# $N^a (\log N)^b$

Input file:	standard input
Output file:	standard output
Time limit:	2 seconds
Memory limit:	1024 megabytes

You are given a function  $F(N)$  for a positive integer  $N$ , represented as a string  $F$  following the BNF notation for the  $\langle \text{expr} \rangle$  symbol as follows:

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 $\langle \text{expr} \rangle ::= \langle \text{term} \rangle \mid \langle \text{expr} \rangle '+' \langle \text{term} \rangle$ 
 $\langle \text{term} \rangle ::= \langle \text{factor} \rangle \mid \langle \text{term} \rangle '*' \langle \text{factor} \rangle$ 
 $\langle \text{factor} \rangle ::= 'N' \mid 'N'^{\langle \text{number} \rangle} \mid 'log(' \langle \text{expr} \rangle ')'$ 
 $\mid 'log(' \langle \text{expr} \rangle ')^{\langle \text{number} \rangle} \mid '(' \langle \text{expr} \rangle ')'$ 
 $\langle \text{number} \rangle ::= \langle \text{nonzero\_digit} \rangle \mid \langle \text{nonzero\_digit} \rangle \langle \text{digit\_string} \rangle$ 
 $\langle \text{digit\_string} \rangle ::= \langle \text{digit} \rangle \mid \langle \text{digit} \rangle \langle \text{digit\_string} \rangle$ 
 $\langle \text{nonzero\_digit} \rangle ::= '1' \mid '2' \mid '3' \mid '4' \mid '5' \mid '6' \mid '7' \mid '8' \mid '9'$ 
 $\langle \text{digit} \rangle ::= '0' \mid \langle \text{nonzero\_digit} \rangle$ 
```

The symbols represent the following:

- $N$ :  $N$
- $+$ : Addition  $+$
- $*$ : Multiplication  $\times$
- $\log$ : Natural logarithm  $\log$
- $(, )$ : Parentheses, with higher precedence than addition  $+$  or multiplication  $*$
- $\wedge$ : Exponentiation, with higher precedence than addition  $+$  or multiplication  $*$

$\langle \text{number} \rangle$  represents an integer in decimal notation, guaranteed to be between 1 and  $10^9$ . Also,  $'log(' \langle \text{expr} \rangle ')^{\langle \text{number} \rangle}'$  represents  $(\log(\langle \text{expr} \rangle))^{\langle \text{number} \rangle}$ .

For example, the following strings can be  $\langle \text{expr} \rangle$  symbols:

- $N+log(N)*N$ : Represents  $N + \log(N) \times N$ .
- $N^1+N^2+log(N)+log(N)^{1000000000}$ : Represents  $N^1 + N^2 + \log(N) + (\log(N))^{1000000000}$ .
- $N*(N+(log(N+N)^2*N))+((N))$ : Represents  $N \times (N + (\log(N + N))^2 \times N) + (((N)))$ .
- $(log((N)))$ : Represents  $(\log((N)))$ .

The following strings cannot be  $\langle \text{expr} \rangle$  symbols:

- $(log(N)+N)^2$ : The form  $'(' \langle \text{expr} \rangle ')^{\langle \text{number} \rangle}'$  is not used in  $\langle \text{factor} \rangle$ .
- $(log(N))^2$
- $(N$
- $)N($

- $N^{10000000001}$
- $N^{0.2}$
- $N^0$
- $N^N$
- 2
- $\log(3)$
- $N - \log(N)$
- $\log(N)/N$

While  $F(N)$  may not be defined for all positive integers  $N$ , for any input, there exists a positive integer  $N_0$  such that  $F(N)$  is defined for all positive integers  $N \geq N_0$ .

Therefore, define the set  $S$  of all non-negative integer pairs  $(a, b)$  such that the limit

$$\lim_{N \rightarrow \infty} \frac{F(N)}{N^a (\log N)^b}$$

converges to a finite value (including 0). Output the **lexicographically smallest pair**  $(a, b)$  in  $S$ .

Here, a non-negative integer pair  $(a, b)$  is the lexicographically smallest in  $S$  if it belongs to  $S$ , and for any other pair  $(a', b')$  in  $S$ , either:

- $a < a'$
- $a = a'$  and  $b \leq b'$

It is proven that  $S$  is not an empty set, and furthermore, there exists the lexicographically smallest pair in  $S$ .

## Input

The input is given from Standard Input in the following format:

$F$

- The function  $F(N)$  is given as a string  $F$  following the  $\langle \text{expr} \rangle$  symbol defined in the problem statement.
- $1 \leq |F| \leq 10^5$

## Output

Output the lexicographically smallest pair  $(a, b)$  of  $S$  separated by a space.

## Examples

standard input	standard output
$N * \log(N^2) * \log(N) + N + \log(N^{1+N})^{2*N}$	1 2
$N * \log(\log(N))$	1 1
$((N)) * N^{234567890} + N^2$	234567891 0

## Note

In the first example,  $F(N) = N \times \log(N^2) \times \log(N) + N + (\log(N^1 + N))^2 \times N$ .

For this case, non-negative integer pairs  $(a, b)$  such that the limit in the problem statement converges to a finite value include  $(a, b) = (1, 2), (1, 3), (2, 0)$ , etc. For these pairs, the limits are as follows:

$$\lim_{N \rightarrow \infty} \frac{F(N)}{N^1(\log N)^2} = 3$$

$$\lim_{N \rightarrow \infty} \frac{F(N)}{N^1(\log N)^3} = 0$$

$$\lim_{N \rightarrow \infty} \frac{F(N)}{N^2(\log N)^0} = 0$$

Note that 0 is considered a finite value. On the other hand, for example,  $(a, b) = (1, 1)$  leads to:

$$\lim_{N \rightarrow \infty} \frac{F(N)}{N^1(\log N)^1} = \infty$$

and does not converge to a finite value.

It can be shown that within the set  $S$  of all pairs satisfying the conditions,  $(a, b) = (1, 2)$  is lexicographically the smallest.

In the second example,  $F(N) = N \times \log(\log(N))$ . For  $(a, b) = (1, 1)$ :

$$\lim_{N \rightarrow \infty} \frac{F(N)}{N^1(\log N)^1} = 0$$

and converges to a finite value.

It can be shown that within the set  $S$  of all pairs satisfying the conditions,  $(a, b) = (1, 1)$  is lexicographically the smallest.

In the third example,  $F(N) = (((N)) \times N^{234567890} + N^2)$ .