## All the Way Left

Input file:
Output file:
Time limit:
Memory limit:
standard input
standard output
2.5 seconds

1024 megabytes

Little Drink Congee is a good friend of Little Cyan Fish and a member of the famous acting group All the Way Left. He has recently been practicing his ability to recognize directions on a stage. To practice, he has selected $n$ distinct points $A_{1}, A_{2}, \cdots, A_{n}$ on the stage. The stage is represented as a two-dimensional Cartesian plane, where the $i$-th point is located at the coordinates $\left(x_{i}, y_{i}\right)$. Little Drink Congee aims to travel through all these points in the order of $p_{1}, p_{2}, \cdots, p_{n}$. A traversal is a permutation $p$ of length $n$, where each point $A_{p_{i}}$ is connected to $A_{p_{i+1}}$ with an oriented line segment.
Little Drink Congee thinks a traversal is considered good if and only if the following condition holds:

- It is non-self-intersecting, i.e. no two segments intersect except for two adjacent segments intersecting at one common endpoint.
- For each $1 \leq i \leq n-2$, the $i$-th turn is left (or going straight). Formally, the cross product of $\overrightarrow{A_{p_{i}} A_{p_{i+1}}}$ and $\xrightarrow[A_{p_{i+1}} A_{p_{i+2}}]{ }$ is non-negative.

Little Drink Congee wants to know the number of good traversals, modulo $\left(10^{9}+7\right)$. However, he needs to spend time with Little Cyan Fish and cannot solve this challenge himself. Please help him calculate it!

## Input

The first line contains a single integer $T\left(1 \leq T \leq 10^{4}\right)$, denoting the number of test cases.
For each test case, the first line contains a single integer $n\left(1 \leq n \leq 2 \times 10^{3}\right)$.
In the next $n$ lines, the $i$-th line contains two integers $x_{i}$ and $y_{i}\left(1 \leq x_{i}, y_{i} \leq 10^{9}\right)$, denoting the coordinates of $A_{i}$. The coordinates of all the points are distinct.
It is guaranteed that the sum of $n^{2}$ over all test cases does not exceed $4 \times 10^{6}$.

## Output

For each test case, output one line, containing the number of good traversals modulo $\left(10^{9}+7\right)$.

## Example

|  | standard input |  |
| :--- | :--- | :--- |
| 3 |  | 6 |
| 4 |  | 2 |
| 1 | 1 | 13 |
| 3 | 1 |  |
| 2 | 2 |  |
| 2 | 3 |  |
| 3 |  |  |
| 1 | 1 |  |
| 1 | 2 |  |
| 1 | 3 |  |
| 6 |  |  |
| 1 | 1 |  |
| 2 | 1 |  |
| 2 | 2 |  |
| 2 | 3 |  |
| 3 | 2 |  |
| 4 | 2 |  |

